

SOCIUS MERCATORIS:  
OR THE *Tanner* 430  
Merchant's Companion:  
IN THREE PARTS.

*The First,*  
Being a plain and easie *Introduction* to  
*Arithmetick*, Vulgar and Decimal;  
the *Extraction* of the *Square* and  
*Cube Roots*, with a Table of 200  
*Square Roots*, and their Use in the  
Resolution of *Square Equations*.

*The Second,*  
A Treatise of *Simple* and *Compound Interest* and  
*Rebate*, with Two Tables for the *Calculation*  
of the Value of *Leases* or *Annuities*, payable  
Quarterly, the one for *Simple*, the other  
*Compound Interest*, at 6 per Cent. per *Annum*,  
with *Rules* for making the like for any other  
Rate.

*The Third,*  
A new and exact way of *Measuring Solids* in the Form  
of a *Prismoid* and *Cylindroid*, with the *Frustrums* of  
*Pyramids* and of a *Cone*: Whereunto is added, some  
*Practical Rules* and Examples for *Cask-Gauging*.

By JOHN MAYNE, Philo-Accomptant.

*Nunquam nimis quod nunquam satis dicitur. Sen.*

LONDON,  
Printed by W. G. for N. Crouch, in *Exchange-Alley*,  
over against the *Royal-Exchange* in *Cornhill*. 1674.

*Thom. Tanner*

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To his Honoured Friend

**THO. WILLIAMS,**

M. D.

*Physician in Ordinary to His S. Majesty.*

---

SIR,



Hough the happiness which I formerly enjoyed in your *Converse*, hath been, to my great loss, for some years discontinued; yet I easily perswade my self,

that the Favour of a *Great Prince*, and the *Best Master* in the World, has not wrought such a change upon your *even Virtue*, but that you will still descend to remember him whom you were once pleased to honour with the Name of *Friend*. This Confidence has emboldned me to present you with this *small*

A 3

*trifle*;

THE EPISTLE DEDICATORY.

*trifle*; too *mean* indeed and *trivial* for your acceptance, but that I know you are wont to admit of any thing that proceeds from an *honest undesigning* Gratitude. And though I am not at all inclin'd to *vanity* from the *merits* of the Work it self, yet I am proud that it affords me an opportunity to discover the *lasting impressions*, which your many *Favours* have made upon my Breast. **Geometry**, with **Arithmetick** her Woman, are Beauties, that having Truth written in their Foreheads, dare appear in the Court of the greatest Monarch, and I doubt not but they will find very easie and courteous admittance into your *Appartment*; where if they shall afford you any divertisement when you return wearied from your *ingenious Elaboratory*, I shall then account that I have written to *very good purpose*. However, they certainly assure you, that it is *impossible* the teeth of Time should obliterate the *honourable esteem* conserved for you, in the heart of,

Sir,  
Your most humble Servant,

JOHN MAYNE.



## THE PREFACE.

**I** Shall not trouble thee, Reader, nor my self, with a long Apology for the publishing this Treatise. How demurely soever I should pretend to the contrary, I fear thou wilt still be apt to imagin, that I had a tolerable good opinion of it, before I ventur'd it to the Press; and truly I my self can't well conceive, how any man should be over ambitious of being publickly laught at. If it be in any measure suited to the General Good, (for which I intended it,) I may at least expect thy pardon; but if upon the perusal thou shalt find it otherwise, I ingenuously acknowledge my self to have been mistaken. My Design in this Work is, to render the Rules of those excellent Arts, which the Title-page pretends to, so plain and obvious, as that they may be easily apprehended without the Assistance of a living Master. And if there were nothing new in the whole, but the perspicuity of the Principles, and easiness of the Method (which out of civility to my self I must deny) yet those alone are sufficient to vindicate me in this Publication; and I hope thou wilt not be angry, that I am a Well-wisher to thy Understanding. For when I consider'd, that among the many good Books of this Nature, that are abroad in the

## THE PREFACE.

World (though written by Persons of greater knowledge than I dare pretend to) some were so learned and obscure, as not to be understood, unless by those who have already made a considerable proficiency in these things; others, so voluminous and prolix that they fright the endeavours of such who cannot spend their whole time this way: I was willing, according to my abilities, to obviate both these inconveniences, and accordingly applied my self to the composition of something, which for its plainness and brevity might be accommodated to those of mean Capacities and small Leisure; and this Book is the result of those Contemplations. Whether I have accomplish'd my purpose or no, I make thee the Judge; requiring only that thou censure impartially of the Author and his Endeavours, without being offended that he is desirous to do thee a courtesie. I shall not here expatiate in the praise of the Arguments I treat of, nor give thee one line of Encomium: though out of the great affection I bear to these Arts, I find a strange inclination in my self to be rhetorical, yet I am resolv'd not to affront thee; for truly their usefulness and excellency is so universally known, that to tell thee of it as a new thing, were to suppose thee a Person of more than ordinary ignorance; only (as I said before) I must be so civil to my self too, as to inform thee, that (besides the Introduction to Arithmetick and the Treatise of Interest, of which I challenge no more than thou shalt find thy self very willing to give me) that Part which concerns the measuring

## THE PREFACE.

*Surving of Solids, viz. the Prismoid, Cylindroid,  
 &c. is wholly new, and never before made publick.  
 The bulk is bigger than at first by me intended;  
 but to gratifie the Book-seller, the Vulgar Arith-  
 metick was an Appendix, though previous to the  
 rest. But if one, or other, or all, prove either  
 profitable or pleasant to thee, I am sufficiently  
 oblig'd to subscribe,*

From my House at the  
 Golden-Ball in Shaws-  
 Court, near St. Georges  
 Church, Southwark;  
 July 29. 1673.

*Thy Friend;*

**John Mayne**

TO THE Ingenious Author, concerning  
his DECIMALS.

- 1 **S**ir, by your Art, and *Pythagorean* Pen,  
I'd prove a *Metempsychosis* agen;  
2 And were His Soul of *Decimals* but made,  
3 As *Plato's* Soul o'th' world of *Seven* is said,  
I'd swear 'twas slunk to you; but that you  
shew  
3 More Skill than e're his rambling fancy  
knew.  
Let roving *Rabbies* praise their *Seven* and  
4 *Four*;  
We'll shew them *Mysteries* enough and more:  
The Heav'nly Orbs are *Ten*, their Motions all  
5 Conspire to make a perfect *Decimal*:  
6 This is their *Musick*, and they shall be thus,  
In spight of *Tycho* or *Copernicus*.  
'Tis said the *Muses* are but *Nine*, but who  
7 (Rather than fail) can't add *Apollo* too?  
Thus may we range the world, and quickly  
find,  
8 We all to th' number of our Fingers bind.  
Thus *Logick* all the wandering *Species* brings,  
9 And places under *tenfold* Heads of *things*.  
Thus I, to give the *Author* praise in all,  
10 Reduce my *Verses* to a *Decimal*.



## On his GAUGING.

**Y**our *Circles*, Sir, would make my folly  
ghes,

You were a *Conjuror*, though you wo'n't confess.

And *Gauging* is the rugged dev'lish Name

Of some *Hobgobling Imp*, the very same

That brought in *Custom*; but what e're he be,

He's a rare Fellow at the *Rule of Three*:

He doth just *square* the *Circle*; nay so true,

That the *King's Right* is given to a *Cue*.

There's none else such *Impossibles* can do:

You give the *King's*, I give this *Right* to you.

J. W.

---

On his worthy Friend Mr. J. Mayne,  
the Author of this BOOK.

Ingenious Artift, whither do'ft aspire?  
Or why t'outvye the Ancients do'ft desire?  
Have they not left enough to following Ages?  
No: Thou their Master art, they but thy  
Pages.

My feeble *Mufe* can never soar fo high,  
As thy Deserts herein extend, nor nigh.  
Yet give me leave hereof to fpeak my mind:  
No Man could better teach us in this kind,  
Each Part fo ufeul, and fo plain I find.

T. W. Φιλομαθ.

---

To his ingenious Friend the Author  
Mr. John Mayne.

Who reads thy Book with an im-  
partial Eye,  
Will see how plain, and how ingeniously  
Thy Rules are fram'd; here every Child may  
learn

*Arithmetick*, which doth the Truth discern.  
The Judges of our Realm could not dispence  
To all Men Justice, were't not fetch'd from hence:  
Those Sons of Mars that furrow Neptune's  
Brow,

Unto this Science must their Labours bow:  
The wealthy Merchant, and all Traders, hence  
Must calculate their Gain, or their Expence:  
The greedy Miser, here may plainly see  
His Pelf's increase at Compound Usurie:  
The Purchaser of Farms, may also here,  
Value his Lordships, whether cheap or deer.  
Thy Squares and Cubes, methinks, so plain do  
seem,

That I old *Euclid* should thy Father deem.  
All Humane Arts, Mechanical and Free,  
For this Companion are oblig'd to Thee.  
By Lines and Numbers, we our Buildings bring  
In due proportion, framing every thing.  
By these our Wooden Walls and Towers are  
fram'd,

Which guard our Island, and the Seas command:  
These

These fill our Stores with rich and costly things,  
 Born from both *Indies* under Canvas Wings :  
 These fortifie our Towns with Forts, by Line ;  
 By these we learn our Foes to undermine :  
 By these th' *Excise* and *Customs* we do scan ,  
 Without *Injustice* to the Trading Man.  
 Thanks to our *Author* then , that hath set forth  
 These *Arts* so plain , and of abundant worth :  
 Which do to Sea and Land such Profit yield,  
 In Court, in City, Garrison, and Field.

Hugh Handy, Philomath.



A

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# ARITHMETICK

IN

## Whole Numbers.

### NOTATION.



It is necessary, that all Persons that would acquaint themselves with the Nature and Use of Numbers, do first learn to know the Characters by which any Quantity is expressed.

These Characters are in number nine, who with a Cypher are the Foundation of the whole Art of Arithmetick: Their form and denomination as in this Example.

0.	1.	2.	3.	4.	5.	6.	7.	8.	9.
Cypher.	One.	Two.	Three.	Four.	Five.	Six.	Seven.	Eight.	Nine.

B

These

These Characters standing alone express no more than their simple value, as 1 is but one, 2 standing by it self signifies but two, and so of the rest; but when you see more than one of those Figures stand together, they have then another Signification, and are valued according to the place they stand in, being dignified above their simple quality, according to the Examples in this Table.

Whole Numbers.								
Hundred Millions.			Hundred Thousands.			Units.		
Ten Millions.			Ten Thousands.			Tens.		
Millions.			Hundreds.			1		
1	2	3	1	2	3	1	2	3
4	5	6	4	5	6	4	5	6
7	8	9	7	8	9	7	8	9
1	2	3	1	2	3	1	2	3
4	5	6	4	5	6	4	5	6
7	8	9	7	8	9	7	8	9

The denomination of Places according to this Table, must be well known, and are thus exprest; those standing in the place of Unites, signifie no more than their value before taught; but standing in the second place toward the left hand, they are increased to ten times the value they had before, 1 or One in the Unite place signifies but One; if it stand in the second place toward the left hand, and a Cypher before

fore it thus 10, it hath ten times its simple value, and is called Ten; if 2 stand in the place of the Cypher thus 12, it is then Twelve, being Ten and two Unites; 1, 2, or 3, standing in third place, with Figures or Cyphers toward the right hand of it, doth signifie Hundreds, as 100 is One hundred, 123 is One hundred twenty three, 321 is Three hundred twenty one, 213 is Two hundred thirteen; and so any three of the other Figures have like value, according to their Stations, the first to the right hand in the Unite place signifies so many Unites, the second, or that in the place of Tens, is increased to ten times its simple value, and in the third place, or place of Hundreds, any Figure there standing hath a hundred times the value it would have had were it in the Unite place.

The fourth place is the place of Thousands, any Figures standing there, with three Figures or Cyphers to the right hand of it, is so many Thousands as simply it contains Unites, so 3000 is Three thousand, 9825 is Nine thousand eight hundred twenty five, &c.

The fifth place is Ten thousands, and any five Figures placed together, are to be read after this manner: *Example.*

45326 Forty five thousand three hundred twenty six.

12345 Twelve thousand three hundred forty five.

The sixth place hath the denomination of  
B 2 Hundred

Hundred thousands, and those six in the Table that stand in a rank are to be read, One hundred twenty three thousand four hundred fifty six.

The seventh is the place of Millions, and the seven in the Table are, One million two hundred thirty four thousand five hundred sixty seven.

And the eighth Rank of Figures are to be read, Twelve millions three hundred forty five thousand six hundred seventy eight.

The ninth rank is, One hundred twenty three millions four hundred fifty six thousand seven hundred eighty nine. And so any greater number of places, every figure one place more toward the left hand, is increased ten times in value more than in the place it stood before.

### *ADDITION.*

**A** *Addition*, is a gathering or collecting of several Numbers or Quantities into one Sum, by placing all Numbers of like Denomination under one another, carrying all above ten to the next place, as in these Examples.

5	56	245	358
6	83	386	876
<u>11</u>	<u>139</u>	<u>194</u>	<u>988</u>
		825	2222
			There



There is likewise another kind of *Addition*, that is not of whole Quantities; wherein is necessary to be known the number of Parts the Integer or whole Number is divided into, as Pounds and Shillings, every Pound is divided into 20 Shillings, and one Shilling is divided into twelve Pence, one Penny into four Farthings.

Now being to add a Number of Pounds and Shillings together, they are thus set down with a small Line or Point between them.

3 - 5

6 : 16

If these be added together, observe in casting up your Shillings, so many times as you have 20 in the Shillings, you must carry Unites to the Pounds, and set down the Remainder, being under 20, as in these Examples.

l. s.		l. s.	
	4:17		4:17
l. s.	3:15		3:15
3:5	5:9		5:9
6:16	6:12		6:12
<hr/>		<hr/>	
10:01	19:13		

In the first Example, I find in adding the Shillings together, they make 21, so I set down 1 and carry 1 Pound to the Pounds: In the second Example, I find among the Shillings 53, which is 2 Pounds 13 Shillings, so I set down 13 under the Shillings, and 2 to the Pounds.

B 3

Any

Any number of Shillings and Pence being to be added together, if your number of Pence amount to above 12, carry 1 to the Shillings, and set down the remainder under the Pence; if they make above 24, carry 2 Shillings, and set down the remainder, as before.

*Examples.*

	s.	d.	
	1	7	
	2	6	
3. d.	8	9	3: 9
1: 6	2	8	4: 8
2: 7	3	10	5: 11
<hr/>	<hr/>	<hr/>	<hr/>
4: 1	15: 03		18: 05

In the first Example, you carry one Shilling; in the second, two; and in the third, three.

In Addition of Pence and Farthings, carry so many times four as you find in the number of Farthings to the Pence, setting down the remainder under the Farthings, as in these Examples.

	d.	q	
	1	3	
	2	2	
	1	1	
d. q	1	2	2: 3
2: 3	3	1	1: 3
3: 2	1	3	1: 2
<hr/>	<hr/>	<hr/>	<hr/>
6: 1	9: 1		11: 2

When

## *Addition.*

When you would know the Sum of any number of Pounds, Shillings, Pence, and Farthing, they are to be placed thus:

l.	s.	d.	q.
15	10	06	2
3	15	10	3
4	12	09	1
<hr/>			
8	08	07	
60	13	02	2

Addition of Weight and Measure is performed after the same manner.

16 Ounces *Averdupois*, make a Pound.

28 Pounds, make a Quarter.

112 Pound, or 4 Quarters, make an Hundred gros.

20 Hundred, make a Tun.

### *Examples.*

C.	qs.	lb.	os.
9	2	24	15
19	3	7	6
15	2	9	15
7	1	18	10
<hr/>			
42	0	08	15
33	3	05	04

Where observe, that so oft as I find 16 Ounces, I carry 1 to the Pounds; so often as I find 28 Pounds, I carry 1 to the Quarters; and as many times as I find 4 in the Quarters, so many times 1 do I carry to the Hundreds.

## SUBTRACTION.

**S**ubtraction is the taking a lesser Number from a greater, and exhibits the Remainder.

In *Subtraction* the Numbers are placed one under another, as in *Addition*, thus :

16

12

—

The first of these Numbers is called the *Minorand*, the second the *Subducend*, and the third Number, or the Number sought, is the *Residuum*.

8 The *Minorand*.6 The *Subducend*.2 The *Residuum* or *Remainder*.

## EXAMPLES of COINS.

	<i>l.</i>	<i>s.</i>	<i>d.</i>		<i>l.</i>	<i>s.</i>	<i>d.</i>
<i>Minorand</i>	8	16	08		45	19	08
<i>Subducend</i>	5	10	07		32	15	06
	<hr/>				<hr/>		
<i>Residuum</i>	3	06	01		13	04	02

But when the number of Pence or Shillings, are greater than the number that stands over it  
in

# Subtraction.

in the *Minorand*, you must borrow the next Denomination, as in this Example,

$$\begin{array}{r}
 \text{L.} \quad \text{s.} \quad \text{d.} \\
 127:01:03 \\
 116:19:09 \\
 \hline
 10:01:06
 \end{array}$$

This Example I work after this manner, saying 9 d. out of 3 d. I cannot have, wherefore I borrow 1 s. from the Shillings, and subduct the 9 d. from that, and there will remain 3 d. which added to the other 3 d. maketh 6 d. I place therefore 6 d. in the Place of Pence, and proceed saying, 1 s. that I borrowed and 19 is 20 from 1 I cannot, wherefore I borrow 1 l. from the Pounds, and subduct from that the 20 s. and there remains nothing but the 1 s. which I place under the Shillings, and say, 1 that I borrowed and 6 is 7 from 7 and there remains nothing, then I place a Cypher under the 6, and say, 1 from 2 and there remains 1, which I set down, and 1 from 1 and there resteth nothing. After this manner is performed *Subduction of Weight and Measure.*

## Examples.

$$\begin{array}{r}
 \text{C.} \quad \text{qs.} \quad \text{lb.} \\
 27:3:15 \\
 16:2:10 \\
 \hline
 11:1:05
 \end{array}$$

$$\begin{array}{r}
 \text{C.} \quad \text{qs.} \quad \text{lb.} \\
 25:1:7 \\
 19:2:12 \\
 \hline
 5:2:23
 \end{array}$$

*Subtraction.*

C.	qs.	lb.	os.			
14	:	1	:	25	:	07
8	:	3	:	27	:	13
<hr/>						
5	:	1	:	25	:	10
<hr/>						

*Proof* 14 : 1 : 25 : 07

---

By which Examples, the Learner may perceive, that where the number to be subducted is greater than the number standing over it, I then borrow one from the next greater denomination, adding the remainder, if any be, to the lesser number before-mentioned, and setting them underneath those of like denomination with them.

The Proof of *Subtraction* is by adding the *Subducend* and *Remainder* together, and their Aggregate must always be equal to the *Minorand*, as you may see by the last Example.

I could here add many more Examples of Weight and Measure, but to the ingenious Practitioner I hope it will be enough, all other being wrought after the same manner, respect being had to the number of lesser denominations contained in each greater. As

*In Troy Weight,*

- 24 Grains make a Penny-weight.
- 20 Penny-weight one Ounce.
- 12 Ounces one Pound.

*Long*



*Subtraction.*

11

*Long Measure.*

- 4 Nails make a Quarter of a Yard.
- 4 Quarters one Yard.
- 5 Nails one Quarter of an Ell.
- 4 Quarters one Ell.
- 12 Inches a Foot.
- 3 Feet a Yard.
- 16½ a Perch.
- 40 Perches a Furlong.
- 8 Furlongs make an *English* Mile.

*Liquid Measure.*

- 8 Pints make a Gallon.
- 63 Gallons make a Graves Hoghead.
- 4 Hogheads make a Tun.
- 36 Gallons make a Beer Barrel.
- 32 Gallons make an Ale Barrel.

*Dry Measure.*

- 8 Gallons of Corn make a Bushel.
- 8 Bushels make a Quarter.

---

*M U L*

## MULTIPLICATION.

**M**ultiplication is a kind of *Addition*, and resolveth Questions to be performed by *Addition* in a different manner: In order whereunto, it is necessary the Learner do well acquaint himself with this Table; the having this Table perfectly by heart, will make both this Rule and *Division* also very facile, otherwise they will be both troublesome and unpleasant.

1	2	3	4	5	6	7	8	9	10	11	12
2	4	6	8	10	12	14	16	18	20	22	24
3	6	9	12	15	18	21	24	27	30	33	36
4	8	12	16	20	24	28	32	36	40	44	48
5	10	15	20	25	30	35	40	45	50	55	60
6	12	18	24	30	36	42	48	54	60	66	72
7	14	21	28	35	42	49	56	63	70	77	84
8	16	24	32	40	48	56	64	72	80	88	96
9	18	27	36	45	54	63	72	81	90	99	108
10	20	30	40	50	60	70	80	90	100	110	120
11	22	33	44	55	66	77	88	99	110	121	132
12	24	36	48	60	72	84	96	108	120	132	144

In the first Rank of this Table, you have an Arithmetical Progression from 1 to 12, and

and also in the first Column toward the left hand downwards. This Table doth at first sight exhibit the Sum of any number, so often repeated as you shall require, provided the numbers do neither of them exceed 12.

*Multiplication* hath three Members, thus called, a *Multiplicand*, a *Multiplicator*, and a *Product*: The *Multiplicand*, is the number to be repeated; the *Multiplicator*, is the number of times the first is to be repeated; and the *Product*, is the Sum of the *Multiplicand* so often repeated. As for *Example*.

*A Countrey-man sold 6 Bushels of Wheat for 5 s. how many Shillings ought he to receive?*

By *Addition* 6 must be 5 times set down thus: Or 5 six times repeated thus:

6	5
6	5
6	5
6	5
6	5
6	5
—	—
30	30

But by *Multiplication* it is done thus:

6	The <i>Multiplicand</i> .
5	The <i>Multiplicator</i> .
—	

Now

*Multiplication.*

Now if you look in the Table precedent ; in the first Column find 5 , then look in the first Rank for 6 , and cast your Eye down to their Angle of meeting, and you will find 30 standing under 6 and against 5 , I then conclude that 5 times 6 is 30 ; that is called the *Product* , and they will stand thus :

6 *The Multiplicand.*

5 *The Multiplier.*

—

30 *The Product.*

But when you have a number to multiply ; greater than any in the Table , as for *Example* :

*A Gentleman having forborn his Rent of a Farm , at 157 l. per Quarter, for 3 Quarters, what ought he to receive ?*

The *Multiplication* will stand thus :

157 *The Multiplicand.*

3 *The Multiplier.*

—

471 *The Product.*

I then say, 3 times 7 is 21 , I set down 1 and carry 2 ; then, 3 times 5 is 15 and 2 is 17 , I set down 7 next the 1 , and carry 1 ; saying, 3 times 1 is 3 and 1 is 4 , as in the Example before-going ; and the *Product* is 471 l.

There

## Multiplication.

15

There is yet more variety, of which take these Examples following.

If 65 Ships do carry 536 Men in every Ship, how many Men will there be in all?

536 The Multiplicand.

65 The Multiplier.

2680

3216

34840 The Product.

I say 5 times 6 is 30, set down 0 and carry 3; then 5 times 3 is 15 and 3 is 18, set down 8 and carry 1; then 5 times 5 is 25 and 1 is 26, which I set down: Then for the next Figure, I say, 6 times 6 is 36, I set down 6 one place short of the former rank, and carry 3; then 6 times 3 is 18 and 3 is 21, set down 1 and carry 2; again, 6 times 5 is 30 and 2 is 32, these I set down: Then draw a line, and cast them up as they are placed, and the Sum is the Product and Answer to the Question, viz. 34840 Men.

In *Multiplication*, always make the lesser Number the *Multiplier*, for it is all one whether I multiply 5 by 15, or 15 by 5, the Product is always the same.

If

If 128 Men of War have each made 746 Shot, how many Shot were made in all?

746
128
—
5968
1492
746
—
95488

Begin as before with the Unites place, and say, 8 times 6 is 48, set down 8 and carry 4; 8 times 4 is 32 and 4 is 36, set down 6 and carry 3; then 8 times 7 is 56 and 3 is 59, which set down: Then go forward with the 2, (but remember to place your remainder one Figure short of the former) saying, 2 times 6 is 12, set down 2 under the 6 and carry 1; 3 times 4 is 8 and 1 is 9, which set down; twice 7 is 14, which set down: Also then, once 6 is 6, which place under the 9; once 4 is 4, which set under the 4; and once 7 is 7, which set under the 1: Then cast them up, as in *Addition*, and the Sum is the *Product*, and answers the Question, viz. 95488 Shot.

If any number be to be multiplied by 1 with Cyphers, it is but adding so many Cyphers to the *Multiplicand* as there is in the *Multiplier*.

*As for Example.*

If 35678 be to be multiplied by 10, add one Cypher to the *Multiplicand*, thus, 356780; if by 100, add two Cyphers, thus, 3567800;

&c.

And



# *Division.*

17

And when any number is to be multiplied by any other number, that hath Cyphers annexed, always place the Cyphers immediately under the Line, as in these Examples.

$$\begin{array}{r} 568 \\ \times 20 \\ \hline 11360 \end{array} \quad \begin{array}{r} 2678 \\ \times 3500 \\ \hline 1339000 \\ 8034000 \\ \hline 9373000 \end{array} \quad \begin{array}{r} 8546 \\ \times 81000 \\ \hline 8546000 \\ 68368000 \\ \hline 69226000 \end{array}$$

## *DIVISION.*

**D***ivision* is also a kind of *Subduction*, and informs the *Querent*, how many times one number is contained in another.

There is in *Division* these three things to be observed, *viz.* the *Dividend*, the *Divisor*, and the *Quotient*. The *Dividend* is a number to be divided into parts, the *Divisor* is the quantity of one of those parts which the former is to be divided by; the *Quotient* is the number of such parts as the *Dividend* doth contain. There is also by accident a fourth number in this Rule necessary to be known, which is a *Remainder*, and that happens when the *Dividend* doth not contain an equal number of such quantities as it is divided by; as when 15 is to

*Division.*

be divided by 4, the *Dividend* is 15, the *Divisor* is 4, and there is a *Remainder* 3.

In Division you may place your numbers thus.

*Dividend.*

Q4. Divisor 4 ) 15 ( 3 Quotient.

00012

### 3 Remainder.

0006478

*Multiplication* is positive, but *Division* is performed by essays or tryals, after this manner:

Here I first inquire

$$35 \overline{) 14665} (4$$

140

6

how many times 3 I can  
have in 14, I find 4  
times, I place 4 in the  
*Quotient*, and then mul-

And, *Method 2* to multiply the *Divisor* by that placing the *Product* underneath the *Dividend*, as in the Example; say, 4 times 5 is 20, set down a Cypher under the 6 and carry 2, then 4 times 3 is 12 and 2 is 14, which I set down also, as in the Example; then subduct this *Product* from the *Figures* standing over them, and set down the *Remainder*.

35) 14665 (41

948

66

35

Then for a new *Dividend*, I bring down the next figure, and postpone that to the *Remainder*, and inquire how many times 3 in 6, I cannot have twice, because I

cannot

# Division.

19

cannot have twice 5 from 5, I say then once, and place 1 in the *Quotient*, proceeding as before saying, once 5 is 5, which I place under the first 6 toward the right hand, and once 3 is 3, which I set down under the other 6; subducting these as the former; I find the Remainder to be 31.

After which I bring down the next figure in the *Dividend*, and postpone it to the Remainder, as in this Example:

Then I inquire how many times 3 in 31, I suppose 9 times, placing 9 in the *Quotient* I multiply again, saying 9 times 5 is 45, 5 and carry 4; then 9 times 3 is 27, and 4 is 31; these being set down, as before directed, and subducted, there will remain nothing. I then conclude, that the *Divisor* is so often contained in the *Dividend* as is expressed in the *Quotient*, viz. 419 times.

For further Instructions, take these Examples.

$$286)6384(24$$

$$\begin{array}{r} 572 \\ \hline \end{array}$$

$$\begin{array}{r} 1164 \\ \hline \end{array}$$

$$\begin{array}{r} 1144 \\ \hline \end{array}$$

$$20$$

$$304)9436(31$$

$$\begin{array}{r} 912 \\ \hline \end{array}$$

$$\begin{array}{r} 316 \\ \hline \end{array}$$

$$\begin{array}{r} 304 \\ \hline \end{array}$$

$$12$$

$$98769$$

C. 2

# Reduction.

8765 ) 87654323 ( 887

790120

864232

790120

741123

691355

49768

32 ) 1400 ( 43

## REDUCTION.

**R**eduction is twofold, viz. bringing greater denominations into smaller, and that by *Multiplication*, as Pounds into Shillings, Shillings into Pence, &c. Also lesser denominations are reduced into greater, by *Division*, as Pence into Shillings, Shillings into Pounds, Minutes into Hours, Hours into Days, and Days into Years, &c.

Having any number of Pounds to reduce into Pence, multiply them by 240.

*Example.*

In 869 Pounds how many Pence?

240

34760

1738

*Ans.* 208560 Pence.

# Reduction.

22

In 2486 Shillings how many Farthings?

48

19888

9944

Ans. 119328 Farthings.

How many Minutes are there in 9476 Hours?

60

The Answer 568560 minutes.

How many Pounds, Shillings, and Pence, are contained in 22929 Farthings?

l. s. d. q

Farthings in 1 l. 960 ) 22929 ( 23; 17; 08; 1

1920

3729

2880

Farthings in 1 s. 48 ) 849 (

48

369

336

Farthings in 1 d. 4 ) 33 (

C 3

21

In 544542 Cubique Inches, how many Beer  
Barrels, Firkins, and Gallons?

Bar. firkin g.

Inches in 1 B. Bar. 10152 ) 544542 ( 53 : 2 : 5  
50760

36942

30456

Inches in 1 Firkin 2538 ) 6486

5076

Inches in 1 Gallon 282 ) 1410

1410

0000

### THE RULE OF THREE.

**T**His Rule is so called, because herein are three numbers given to find a fourth; of these three numbers, two are always to be multiplied together, and their Product is to be divided by the third, and the Quotient exhibits the fourth number, or the number sought.

And here note, That of the three given numbers, if that number that asketh the Question be greater than that of like denomination with it self, and require more, or if it be less, and require less, then the number of like denomination is the Divisor.

# The Rule of Three.

23

Or, if the number that asketh the Question be less than that of like denomination, and require more; or if it be more, and require less, then the number that asketh the Question is the Divisor.

## Example.

If 3 Yards of Sarcenet cost 15 s. what shall 32 Yards cost?

Which 3 numbers if you please may stand thus :

$$3 \cdot 15 :: 32$$

$$15$$

$$160$$

$$32$$

$$3)480(160$$

$$3$$

$$180$$

Here you may see the term that asketh the Question is greater than that of like denomination, being 3, and the other 32, and also requires more, viz. a greater number of Shillings; therefore, according to the Rule, the first term, or the term of like denomination to that which asketh the Question, is the Divisor.

C 4

And



# *The Rule of Three.*

And the Answer is 160 Shillings, which being divided by 20 will be found 8 l.

Again,

If 32 Ells of Holland cost 160 s. what shall 3 Ells cost?

$$32 . 160 :: 3$$

$$32 \overline{) 480} (15$$

$$32$$

$$160$$

$$160$$

$$0$$

In this Question (being the Converse of the former) you may see the term that asketh the Question, here 3, is lesser than that of like denomination, being 32 Ells, and also requires less; therefore the first term here also is the Divisor.

And the Answer is 15 s.

If 36 Men dig a Trench in 12 Hours, in how many Hours will 144 Men dig the same?

$$36 . 12 :: 144$$

$$12$$

144 ) 432 ( 3 Hours, the fourth number.

$$432$$

$$000$$

In

# The Rule of Three.

35

In this Question, the term that asketh the Question is greater than that of like denomination, and requireth less; wherefore the term that asketh the Question is the Divisor.

If 144 Workmen build a Wall in 3 Days, in how many Days will 36 Workmen build the same?

$$144 : 3 :: 36$$

$$3 : 2 :: 2 : 3$$

$$36 \overline{) 432} ( 12 \text{ Days.}$$

$$36$$

$$72$$

$$72$$

$$00$$

This Question you may perceive to be the Converse of the former, here the term that asketh the Question is less than that of like denomination, and requires more, the term that asketh therefore is the Divisor.

If 125 lb. of Bisket be sufficient for the Ships Company for 5 Days, how much will Victual the Ship for the whole Voyage, being 153 Days?

This Question is of the same kind with the first Example; here the two terms of like denomination

nomination are 5 Days and 153 Days, the term that asketh the Question being more than the term of like denomination, and also requiring more; so, according to the general Rule, the term of like denomination to that which asketh the Question is the Divisor. It matters not therefore in what order they are placed, so you find your true Divisor; but if you will you may set them down thus :

$$125 \cdot 5 :: 153$$

$$125$$

$$765$$

$$306$$

$$153$$

$$5 \mid 19125 (3825$$

$$15$$

$$41$$

$$40$$

$$12$$

$$10$$

$$25$$

$$25$$

$$00$$

The Answer is 3825 lb. weight of Bisket.

A Ship having Provision for 96 Men during the Voyage, being accounted for 90 Days, but the Master taking on board 12 Passengers, how many Days Provision more ought he to have?

Which is no more than this :

If 96 Men eat a certain quantity of Provision in 90 Days, in how many Days will 108 Men eat the same quantity?

$$96 \cdot 90 :: 108$$

$$\begin{array}{r} 96 \\ \hline \end{array}$$

$$540$$

$$810$$

$$108 \cdot 8640 \cdot 80$$

$$864$$

$$\begin{array}{r} 0000 \end{array}$$

The Answer is 80, so that for 108 Men he ought to have 10 Days Provision more.

If the Assize of Bread be 12 Ounces, Corn being at 8 s. the Bushel, what ought it to weigh when it is sold for 6 s. the Bushel?

$$8 \cdot 12$$

8 . 12 : 16

8

—

6) 96 (16

6

—

36

36

—

00

In this Question, the term inquiring being less than the term of like denomination, and requiring more, therefore is the term so inquiring the Divisor.

The Answer is 16 Ounces.

## THE RULE OF PRACTICE.

IT is necessary that the Learner get these two Tables perfectly by heart, which are only the aliquot parts of a Pound and of a Shilling.

<i>The Parts of a Shilling.</i>		
<i>d.</i>	<i>q.</i>	
0	1	Forty eighth.
0	2	Twenty fourth.
0	3	Sixteenth.
1	0	Twelfth.
1	2	Eighth.
2	0	Sixth.
3	0	Fourth.
4	0	Third.
6	0	Half.

*The*

The Parts of a Pound

s.	d.	q.	
0	00	1	The Nine hundred and sixtieth.
0	00	2	The Four hundred and eightieth.
0	00	3	The Three hundred and twentieth.
0	01	0	The Two hundred and Fortieth.
0	02	0	The Hundred and sixtieth.
0	02	0	The Hundred and twentieth.
0	03	0	The Eightieth.
0	04	0	The Sixtieth.
0	05	0	The Forty eighth.
0	06	0	The Fortieth.
0	08	0	The Thirtieth.
0	10	0	The Four and twentieth.
1	00	0	The Twentieth.
1	03	0	The Sixteenth.
1	04	0	The Fifteenth.
1	08	0	The Twelfth.
2	00	0	The Tenth.
2	06	0	The Eighth.
3	04	0	The Sixth.
4	00	0	The Fifth.
5	00	0	The Fourth.
6	08	0	The Third.
10	00	0	The Half.

Having these Tables perfectly in memory,  
any Question propounded will be readily re-  
solved, only by dividing the given number of  
Yards,

Yards, Ells, Feet, Inches, Gallons, Quarts,  
Pounds, or Ounces.

*Of which take some Examples.*

145 Ells of Cloth at Three Pence being  
3 d. per Ell. the fourth part of a  
36 s. 3 d. Shilling, I divide the  
number by 4; and the  
quote is the number of  
Shillings it is worth.

728 at 4 d.

Four Pence being the  
third part of a Shilling;  
I divide by 3.

242 s. 8 d.

654 at 6 d.

Here take the half.

327 s.

321 at 1 d. 2 q.

Here the eighth part.

40 s. 1 d. 2 q.

542 at 2 d. 1 q.

Here take the sixth  
and the eighth part of  
the quote.

90 : 4 : 0

11 : 3 : 2

101 s. 7 d. 2 q.

Having any number of Shillings to reduce  
into Pounds, cut off the last figure toward the  
right



# The Rule of Practice.

31

right hand by a line, and the figures on the left hand of the line are so many Angels as they express Unites; draw a line under them, and take the half of them, and you have the number of Pounds.

## Examples.

l. s. d.	l. s. d.	l. s.
36:03	24:2:08	32:7
<hr/>	<hr/>	<hr/>
16:03	12:02:08	16:07

l. s. d. q

4:0:01:2

---

2:00:01:2

l. s. d. q

10:1:07:2

---

5:01:07:2

Any Commodity, the value of 1 Yard being the aliquot part of a Pound, is thus cast up:

836 Yards of Broad Cloth at 6 s. 8 d. per Yard.

278 l. 13 s. 4 d.

Take the one third part, and that is the Answer in Pounds; in 8 twice, and carry 2; 3 in 23 seven times, and carry 2; 3 in 26 eight times, and carry 2; the third part of 2 l. is 13 s. 4 d. where always observe, that the Remainder is always of the same denomination with the Dividend.

654 lb. of Cloves at 5 s. per lb. **Take the fourth part.**  
 163 l. 10 s.

9464 Gall. of Brandy at **The Sixth.**

3 s. 4 d.  
 1577 l. 6 s. 8 d.

Where the Price is not aliquot.

625 at 3 s. per Ounce. **Here I take the tenth and the half of that tenth.**

62 : 10 s.

31 : 05 s.

93 : 15

348 Dollers at 4 s. 6 d. **The fifth and the eighth of that fifth.**

69 l. 18 s.

8 : 14

78 : 06

245 lb. at 2 s. 3 d. **The tenth and the eighth of that quote.**

24 : 10 s.

3 : 10 s. 03

27 : 11 s. 03

To cast up the amount of any Commodity sold for any number of Farthings by the Pound,

I borrow from the *Dutch* a Coin called a *Guilder*, whose value is 2 *s. English*.

Then if a Question be proposed of the Amount of an Hundred weight of any Commodity, by the Hundred Groſs, viz. 112 lb. ſo many Hundred as there be, the Amount is ſo many Guilders ſo many Groats, as there are Farthings in the price of 1 lb.

*As for Example.*

A Hundred weight of Iron is ſold for 5 Farthings the Pound, comes to 5 Guilders, that is 10 *l.* and 5 Groats, which together is 11 *s.* 8 *d.*

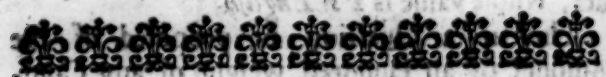
*Again.*

A Hundred weight of Lead is ſold for 2 *d.* Farthing the Pound, that is 9 Guilders and 9 Groats, which is 21 Shillings.

But if it be the ſubtil Hundred, it is then but ſo many Guilders ſo many Pence: As if a Hundred weight of Tobacco be ſold for 5 *d.* Farthing the Pound, the Hundred comes to twenty one Guilders and twenty one Pence, that is forty three Shillings and nine Pence.

to nine of the whole Numbers, the value of  
denomination of Places do increase  
by Tens, from the Unit place toward  
the left hand in Decimals, the  
value of denomination of Places do decrease  
by

**A**  
**ARITH**



# ARITHMETICK

## IN

### DECIMALS.

#### NOTATION.

<i>Integers.</i>										<i>Decimals.</i>									
3	9	8	7	6	5	4	3	2	1	.	2	3	4	5	6	7	8	9	0
Thousand Millions.										Thousand Millioneths.									
Hundred Millions.										Hundred Millioneths.									
Ten Millions.										Ten Millioneths.									
Million.										Millioneths.									
Hundred Thousandths.										Hundred Thousandths.									
Ten Thousandths.										Ten Thousandths.									
Thousandths.										Thousandths.									
Hundredths.										Hundredths.									
Tenths.										Tenths.									
Units.										Units.									
Tens.										Tens.									
Hundred.										Hundred.									
Thousand.										Thousand.									

**A**S in Whole Numbers, the value or denomination of Places do increase by Tens, from the Unite place toward the left hand. So in Decimals, the value or denomination of Places do decrease by

by Tens, from the Unite-place toward the right hand, according to the precedent Table.

A Fraction or broken Number is always less than a Unite, as Pence are parts of a Shilling, and Shillings of a Pound, Inches of a Foot, and Minutes of an Hour.

Fractions are of two kinds,

And are thus called  $\left\{ \begin{array}{l} \text{Vulgar,} \\ \text{\&} \\ \text{Decimal.} \end{array} \right.$

A vulgar Fraction is commonly expressed by two Numbers set over one another, with a small line between them, after this manner  $\frac{1}{2}$ , the uppermost being called the Numerator, and the lower the Denominator.

The Denominator expresseth into how many parts the Integer or whole Number is divided, and the Numerator sheweth how many of these parts is contained in the Fraction.

Example.

If the Integer be a Shilling, it is 12 d.

If it be 1 £ or 20 Shillings, it is 12 s. 4 d.

If a Foot, it is then 12 Inches.

Or if an Hour, it will be 60 Minutes.

A decimal Fraction hath always 9 common Number for a Numerator, and a decimal Number for its Denominator.

A decimal Number is known by Unity, with one

one or more Cyphers standing before it, as 10, 100, 1000, &c.

A *decimal Fraction* is known from a whole Number by a point, or some other small mark of distinction, whether it stand alone, or be joyn'd with whole Numbers; as in these following Examples.

.3275      3.275      32.75      327.5

15653      51653      56153      56513

Or else with a point over the head of Unity, or the Unite place, as in these Examples.

03275      3275      3275      3275

In *decimal Fractions*, the Numerators only are set down, the Denominator being known by the last Figure in the Numerator.

### Example.

.2 is Two tenths.

.25 is Twenty five Hundredths.

.257 is Thousandths.

.2579 is Ten Thousandths; &c.

As Cyphers before a whole Number have no value, so Cyphers after a *decimal Fraction* are of no signification: But Cyphers before a *decimal Fraction*, are of special regard; for

# *Addition.*

17

as Cyphers after a whole Number do increase that Number, so before a *decimal* Fraction they diminish the value of that Fraction.

*Example.*

.25 Twenty five hundredths.

.025 Twenty five thousandths.

.0025 Twenty five ten thousandths.

Each Cypher so added removing the Fraction further from Unity; making it ten times less than before.

85

24.2

278.

202.1

210.

827.

*ADDITION.*

507.

**A**ddition in Decimals, whether in pure Decimals, or whole Numbers mixt with Decimals, differs not from *Addition* in whole Numbers, only care must be had to the separating lines or points, that all places of like denomination stand one under another, both in the Addends and in the Sum; as in these Examples.

.359

.201

55.675

.432

.032

2.031

.352

.103

1.009

.816

.005

31025

1.959

.341

60.740

D 3

SHE-



## SUBTRACTION.

**A**S in *Addition*, so in *Subtraction* care must be had to the placing each Figure under that of like denomination with it self, then it is the same with *Subtraction* in whole Numbers.

## Examples.

$$\begin{array}{r} 875 \\ - 368 \\ \hline 507 \end{array} \qquad \begin{array}{r} 5.43 \\ - .215 \\ \hline 5.215 \end{array} \qquad \begin{array}{r} 28 \\ - 1.565 \\ \hline 26.435 \end{array}$$

$$\begin{array}{r} 243 \\ - 257 \\ \hline 242.743 \end{array} \qquad \begin{array}{r} 35 \\ - 100375 \\ \hline 34.99625 \end{array}$$

## MULTIPLICATION.

**M**ultiplication in whole Numbers serveth instead of many *Additions*, and teacheth of two Numbers given to increase the greater as often as there are Unites in the lesser.

It likewise consists of three Requisites, viz. a *Multiplicand*, a *Multiplicator*, and a *Product*.

The

The *Multiplicand* is the Number to be increased.

The *Multiplier* is the Number by which it is to be increased.

And the *Product* is the Sum of the first Number so often repeated as there are Units in the second.

In decimal Fractions, or whole Numbers mixt with Fractions, the two first Numbers are called *Factors*, and the last is called the *Fact*.

*Multiplication*, whether in decimal Fractions, or whole Numbers mixt with Fractions, differeth not (in the Operation) from *Multiplication* in whole Numbers. The last Figures in both the *Factors* may be placed under one another, without respect to the distinction of places, or places of like denomination standing under one another, as in *Addition* and *Subtraction*; yet from the *Product* must be cut off by a line or point so many places as there are Figures in decimal Fractions in both *Factors* of the last Figures standing toward the right hand.

*Examples.*

$$\begin{array}{r} .25 \\ 3 \\ \hline \end{array}$$

$$\begin{array}{r} .459 \\ 3.6 \\ \hline \end{array}$$

$$\begin{array}{r} 6.25 \\ .5 \\ \hline \end{array}$$

$$\begin{array}{r} 25 \\ 8.5 \\ \hline \end{array}$$

$$.75$$

$$\begin{array}{r} 2754 \\ 1377 \\ \hline 1.6524 \end{array}$$

$$3.125$$

$$\begin{array}{r} 125 \\ 200 \\ \hline 212.5 \end{array}$$

D 4

If

If it happen when the *Multiplication* is ended, that there be fewer Figures in the *Product* than there are places in Decimals in both the *Factors*, then put Cyphers before the *Product* till the number of places be equal to those in both the *Factors*: As in these;

## Examples.

$$\begin{array}{r} .0275 \\ \times .02 \\ \hline .000550 \end{array} \quad \begin{array}{r} .06 \\ \times .4 \\ \hline .024 \end{array} \quad \begin{array}{r} .3 \\ \times .2 \\ \hline .06 \end{array} \quad \begin{array}{r} .8 \\ \times .3 \\ \hline .24 \end{array}$$

Whereby may be observed, That the *Multiplication* of two Fractions doth not increase them as in whole Numbers, but they are hereby made less, and the *Point* is removed further from Unity than either of the *Factors*.

If a whole Number be to be multiplied by a decimal Number, put so many Cyphers after the whole Number as there are in the decimal Number, and that Number will be the *Product*. If 48 be multiplied by 10, it will be 480; by 100, 4800; &c.

In multiplying decimal Fractions, or mixt Numbers, by a decimal Number, you need only remove the point or separating line so many places toward the right hand as there be Cyphers in the decimal Number. If you multiply .2845 by 10, the *Fact* will be 2.845; by 100, it will be 28.45; by 1000, 284.5; &c.

**DIVISION.**

**D**ivision, both in whole Numbers and Fractions, is by young Practitioners found to be more difficult than any of the four Species; it will therefore require a little more industry in the Learner: But when once had, there will appear small difference between the Operation herein, as in any the precedent.

Division is also constituted by three Requisites, and a fourth by accident, viz. a *Dividend*, a *Divisor*, and a *Quotient*: The fourth is a *Remainder*, which doth not always happen to be.

The *Dividend* is the Number to be divided.

The *Divisor* is the Number by which the other is to be divided.

The *Quotient* is the Number found out by the Division.

And the *Remainder* is that which is left of the Dividend after the Division is ended, and is always less than the Divisor.

**Example.**

If 12 be to be divided by 4, then is 12 the Dividend, 4 the Divisor, and the Quotient will be 3.

If 13 be divided by 3, then 13 is the Dividend, 3 the Divisor, 4 the Quotient, and there will be a Remain, which is here 1.

De-

Decimal Fractions, or mixt Numbers, are divided after the same manner as whole Numbers are divided, only care must be had in giving a true value to the Quotient. To perform which, observe well this General Rule.

*The first Figure in the Quotient is always of the same denomination with that Figure which stands (or is supposed to stand) over the Unity place in the Divisor.*

As to the manner of placing your Figures, and the way of dividing, these are many published by divers Writers of *Arithmetick*: The way of placing the Divisor under the Dividend, is the most apt for giving a value to the Quotient; but the raising of Figures, and repeating the Divisor so often, is found an inconvenience; which to avoid, observe the following Examples.

Being to divide 2487.04 by 53.6, I place them in this order;

$$53.6 \overline{) 2487.048}$$

Then I consider if the Divisor were placed under the Dividend, the Unity place in the Divisor, here 3 would stand under the 8 in the Dividend, I then set a mark over the head of the 8, and conclude the first Figure in the Quotient to be of the same denomination with 8, which is Tens, in whole Numbers.

# Division.

43

53.6) 2487.048 (4

343

Having thus found the value of the first Figure in the Quotient, I proceed to the division, and inquire, how many times 5 in 24? I find 4; I then set 4 in the Quotient, and go back, multiplying the whole Divisor by that Figure, and subduct the Product out of the Dividend, placing the Remainder underneath as part of a new Dividend: Thus 4 times 6 is 24, from 27, and there remains 3, which I place under the 7; again, 4 times 3 is 12, and 2 that I borrowed is 14, from 18, and there remains 4, which I place under the 8, as in the Example; then 4 times 5 is 20, and 1 I borrowed is 21, from 24, and there remains 3, which I place under the 4. For my new Dividend, I bring down the next Figure, here a Cypher, and postpone it to the Remainder, and the Example will stand thus:

53.6) 2487.048 (4

343 0

Then proceeding in my Division, I ask, how many times 5 in 34? finding 6 times, I then place 6 in the Quotient, and as before say, 6 times 6 is 36, from 40, and there remains 4, which I set down under the Cypher; then 6 times 3 is 18, and 4 I borrowed is 22, from 23, and



and there remains 1, which I place under the 3; then 6 times 5 is 30, and 2 I borrowed is 32, from 34, and there will remain 2, which I place under the 4; then to this Remainder I bring down the next Figure in the Dividend, postponing it as I did the Cypher, and they will stand thus:

$$\begin{array}{r} 53.6 \overline{) 2487.048} \\ \underline{2580} \phantom{00} \\ 607 \phantom{00} \\ \underline{600} \phantom{00} \\ 70 \phantom{00} \\ \underline{70} \phantom{00} \\ 80 \phantom{00} \\ \underline{80} \phantom{00} \\ 00 \phantom{00} \\ \underline{00} \phantom{00} \\ 80 \phantom{00} \\ \underline{80} \phantom{00} \\ 00 \phantom{00} \end{array}$$

I now inquire, how many times 5 in 21, 2, and find 4 times, I then place 4 in the Quotient, and go on as before; there being yet a Remainder, I add a Cypher, and proceed as before; and find, upon the adding one Cypher, my Divisor greater than the Dividend, I place a Cypher in the Quotient: Example.

$$\begin{array}{r} 53.6 \overline{) 2487.048} \\ \underline{2580} \phantom{00} \\ 607 \phantom{00} \\ \underline{600} \phantom{00} \\ 70 \phantom{00} \\ \underline{70} \phantom{00} \\ 80 \phantom{00} \\ \underline{80} \phantom{00} \\ 00 \phantom{00} \\ \underline{00} \phantom{00} \\ 80 \phantom{00} \\ \underline{80} \phantom{00} \\ 00 \phantom{00} \end{array}$$

Having placed a Cypher in the Quotient, I add another to the Dividend, and make it 800; and then inquire, how many times 5 in 8? finding once, I put 1 in the Quotient, working as before: Where note, So long as there is a Remainder, if you add Cyphers and work after this manner, you may have as many Decimals as you please.

It



# *Division.*

45

It doth often happen in Division, in decimal Fractions, or mixt Numbers, that the Unite place in the Divisor will stand beyond all the significant Figures in the Dividend, either toward the right hand or toward the left; in which case, that you may the better find out the value of the first Figure in your Quotient (according to the precedent General Rule) add Cyphers to the right or to the left hand of the Dividend, till you come over the Unity place in the Divisor, and what value or denomination that place is of, that is the denomination of the first Figure in the quote; as in these

## *Examples.*

$$\begin{array}{r} 254 \overline{) 21.00} (.0826 \\ \underline{680} \\ 1720 \\ \underline{196} \end{array}$$

$$24 \overline{) 7.2} (.3 \\ \underline{0}$$

$$\begin{array}{r} 3.42 \overline{) 1681} (783.9 \\ \underline{2870} \\ 1340 \\ \underline{3140} \\ 62 \end{array}$$

If you divide 66 by 8, the quotient will be 8, according to the way of vulgar Fractions.

$$4275 \overline{) 0351 (12763}$$

760

2100

1750

1000

175

$$42.25 \overline{) 354.375 ( 8.373}$$

16 375

3 1000

14250

1575

$$.025 \overline{) 0.225 ( 9}$$

00

$$.08375 \overline{) 025.750 ( 307.4}$$

62500

38750

$$.002 \overline{) 001.6 ( 500}$$

If in Division in whole Numbers, there happen to be a Remainder, it is the Numerator of a Common Fraction, and the Divisor is the Denominator, and this Fraction is part of the quotient.

*Example.*

If you divide 66 by 8, the quotient will be 8 and  $\frac{2}{8}$ , according to the way of Vulgar Fractions,

Fractions, but in Decimal Fractions it will be 8.25.

*Common way.*

$$8 \overline{) 66} ( 8 \frac{2}{8}$$

*Decimal way.*

$$8 \overline{) 66} ( 8.25$$

If you be to divide a whole by a decimal Number, cut off so many places by a mark, as there are Cyphers in the decimal Number: If 468 be divided by 10, the quote is 46.8; by 100, 4.68; and by 1000, quotes .468.

If a decimal Fraction, or a mixt Number, be to be divided by a decimal Number, remove your line or point so many places toward the left hand, as there are Cyphers in your decimal Number, supplying the vacant places with Cyphers, if there be occasion: 69.5 divided by 10, is 6.95; by 100, it will be .695; by 1000, .0695; and by 10000, quotes .00695; &c.

*Division being the Converse of Multiplication*, as multiplying a mixt Number or decimal Fraction by a decimal Number, you remove your mark of distinction toward the right hand; so in dividing a decimal Fraction or mixt Number by a decimal Number, the mark is removed toward the left hand, as in the foregoing Examples.

## REDUCTION.

**T**O reduce a vulgar Fraction into a decimal Fraction, your Rule is: *Divide your Numerator by your Denominator, and the Quotient will be a decimal Fraction of the same value with the vulgar Fraction.* So  $\frac{1}{4}$ , if reduced into a decimal Fraction, will be .25.

*Example.*

$$\begin{array}{r} 4 \overline{) 1.0} \quad (.25) \\ \underline{40} \phantom{0} \\ 0 \end{array}$$

Here note, That only the even parts of an Integer will be exactly reduced into a decimal Fraction, as  $\frac{1}{2}$ ,  $\frac{3}{4}$ ,  $\frac{5}{8}$ , &c. In all Surds, there will be some Remainder, but if you carry your decimal Fraction to four or five places, making the last one more than it is, if the sixth Figure be above 5, or else leave them out, and your Calculation will come near the truth, but if any desire to be more exact, he may take as many as he please.

*Ex.*

*Reduction.*

*Examples.*

$$\frac{1}{3} \quad 3) 1.0(.33333$$

3) 2.0(666666  
20  
20  
20  
20  
20  
—  
2

$$\begin{array}{r} \frac{1}{7} \quad 7(3.0(.428571 \\ \quad \quad 20 \\ \quad \quad 60 \\ \quad \quad 40 \\ \quad \quad 50 \\ \quad \quad 10 \\ \hline \quad \quad 30 \end{array}$$

$$\begin{array}{r} 20 \\ 20 \\ 20 \\ \hline 20 \end{array}$$

To reduce any decimal Fraction out of a greater denomination into a lesser, multiply the Fraction by those parts of the Integer into which you would have it reduced; as .65 being the parts of a Pound, you would know how many Shillings are contained in the Fraction, multiply it by 20: If you desire the Pence therein contained, multiply it by 240; or if Farthings, multiply by 960, the number of Farthings in a Pound or 20 Shillings.

$$\begin{array}{r}
 .65 \\
 6000 \ 20 \\
 \hline
 13.00 \\
 \text{Answ. } 13 \text{ s.}
 \end{array}$$

$$\begin{array}{r}
 .65 \\
 240 \\
 \hline
 2600 \\
 1300 \\
 \hline
 156.00 \quad \text{Answ. } 156 \text{ d.}
 \end{array}$$

$$\begin{array}{r}
 .65 \\
 960 \\
 \hline
 3900 \\
 985 \\
 \hline
 624.00 \quad \text{Answ. } 624 \text{ q.}
 \end{array}$$

The decimal parts of a Foot are reduced, by multiplying them by 12; if parts of a Foot Square, by 144; and the decimal parts of a Foot Solid, by 1728, the Cubick Inches in a Foot of Solid. The decimal parts of a Pound, are reduced by 16, the Ounces in a Pound *Averdupois*; and 12, the Ounces in a Pound *Troy*. The decimal parts of a Beer Barrel by 36, and by 32 reduceth the parts of an Ale Barrel, into Gallons; and Gallons into Pints, by 8; Gallons into Cubick Inches, by 282; and for Wine Gallons, by 231, the number of Cubick Inches in such a Gallon, &c.

As greater denominations are reduced to lesser, by a multiplication of the several parts of the Integer; so lesser denominations are reduced

# Reduction.

51

reduced to greater; by division. Any number of Shillings are reduced into Pounds, and the decimal parts of a Pound; if you divide them by 20; and Pence; if divided by 240.

## Example.

$$\begin{array}{r} \text{£} \quad \text{s} \quad \text{d} \\ 20 \overline{) 15.0} (.75 \end{array}$$

$$\begin{array}{r} \text{£} \quad \text{s} \quad \text{d} \\ 240 \overline{) 180.0} (.75 \end{array}$$

Hours are reduced into the decimal parts of a Day, if you divide them by 24, the Hours in a Day Natural; and Minutes into the parts of an Hour, if divided by 60:

Perches are reduced into the decimal parts of an Acre, if you divide them by 160, the number of Square Poles or Perches in an Acre; and any number of Feet into Poles, and the decimal parts of a Pole, if you divide them by 16.5 the Feet in a Pole, or by 158.25 the number of Square Feet in a Square Pole; but if Wood-land Measure by 18, or if a Square Pole by 324; the Square Feet in a Pole or Perch of such Measure.

Any number of Inches are reduced into the parts of a Beer Barrel, if divided by 10152; and into Ale Barrels and parts, by 9024; &c.

For the ease of the Reader here is made a Table of *English* Coin reduced into the decimal parts of a Pound *sterling*.



*A Table of Reduction of English Coin,  
the Integer being one Pound.*

<i>Shil- lings.</i>	<i>Deci- mals.</i>		<i>Pence.</i>	<i>Decimals of a Pound.</i>
19	.95		11	.0458333
18	.9		10	.0416667>
17	.85		9	.0375
16	.8		8	.0333333<
15	.75		7	.0291667>
14	.7		6	.025
13	.65		5	.0208333
12	.6		4	.0166667>
11	.55		3	.0125
10	.5		2	.0083333<
9	.45		1	.0041667>
8	.4			
7	.35			
6	.3			
5	.25			
4	.2			
3	.15			
2	.1			
1	.05			
		<i>Far- things.</i>		<i>Decimals of a Pound.</i>
		3		.003125
		2		.0020833
		1		.0010417>

## The Use of the Table.

Having any Quest. wherein Pounds, Shillings & Pence, are required to be under one denomination, viz. Pounds, and the parts of a Pound: First seek in the Column of Shillings for your Shillings, and set down the Fraction that stands against it; then in the Column of Pence, seek your Pence; in the Farthings, your Farthings; add all these together, and the Sum is the decimal Fraction desired.

## Example.

What is the decimal Fraction for 17 s. 9 d.  $\frac{3}{4}$

First as the decimal parts of a Pound seek for 17 s. and the Fraction against it in the other Column is .85;

Which set down thus ——— .85

Then against 9 d. I find ——— .0375

And against 3 Farthings ——— .003125

Their Sum is ——— .890625

Which is the Number required, and is the decimal Fraction for 17 s. 9 d.  $\frac{3}{4}$ , as parts of a Pound.

Again, having a decimal Fraction in the parts of a Pound, and its desired to know the value thereof in lesser denominations: Let it be the Fraction before found, viz. .890625: I seek in the Table of Fractions for the nearest to it,

and find .85, and against it 17 s. I then set .85 down, and subduct it from the other, and there remains .040625; I look over the Table again, and find the next neereſt is .0375, againſt it 9 d. I ſubduct that; and find the Remainder .003125, ſtand againſt 3 Farthings.

$$\begin{array}{r}
 .890625 \\
 .85 \\
 \hline
 .040625 \\
 .0375 \\
 \hline
 .003125
 \end{array}$$

So finding the value of any other decimal Fraction: If any thing remain after the laſt ſubduction, being leſs than a Farthing, I caſt it away as of ſmall regard.

### THE GOLDEN RULE.

**T**His Rule is called the *Rule of Three*, be-  
 cauſe herein are three Numbers given, to  
 find a fourth. It is alſo called the *Rule of Pro-  
 portion*, for as the firſt is in proportion to the  
 ſecond, ſo is the third to the fourth: And the  
*Converſe*.

This Rule is called the *Golden Rule* for its  
 excellent uſe in the Solution of Questions of  
 various kinds, and great advantage is made of it  
 in almoſt all kind of Calculations Arithmetical.

Two of the three Numbers given in every Rule of Proportion are of one denomination, and the third is of the same kind with the fourth sought; and one of the two Numbers that are of like *species* doth always ask the Question.

*Arithmeticians* distinguish this Rule by two denominations, one they call the *Direct*, and the other the *Inverse* or *Backer Rule of Three*.

One of the three given Numbers of like denomination in any Rule of Proportion is a Divisor, the other remaining two are Multipliers. To find which of the forementioned Numbers is the Divisor, take these following Rules.

1. If that Term to which the Question is annexed be more than that of like denomination, and also requires more; or if it be less, and require less than the Term of like denomination; then that Term of like denomination to that which asketh the Question is the Divisor, and the Question is in the *Direct Rule of Three*.
2. If the Term which asketh the Question be more than that of like *species*, and requires less; or less, and requires more; then that Term which asketh the Question is the Divisor, and the Question is in the *Backer* or *Inverse Rule of Three*.

Having by the precedent Rules discovered the Divisor, multiply the other two Numbers, and

divide by the Divisor, your quote will be the Answer to the Question.

*Note,* If any of the Numbers given be in several denominations, they must be reduced into one, either greater or lesser, as before directed.

*Example.*

**Quest. 1.** If  $12 \frac{1}{2}$  Yards of Taffaty cost 5 l. 7 s. 9 d. 3 q. what shall  $5 \frac{1}{2}$  Yards cost?

In this Example, of the three Numbers given there are two of like denomination, and they are  $12 \frac{1}{2}$  and  $5 \frac{1}{2}$ , the latter of which is the Term which asketh the Question, known always by the words *what* or *how much*. And this Term is less than that of like kind with it self, and also requires less, therefore according to the precedent Rule, this Question is in the *Golden Rule Direct*. These three Numbers may be placed in what order you please, provided you mistake not your Divisor, but according to the general way, being reduced into Decimals, and of one species, they will stand thus:

Yards. l. Yards.  
12.5 . 5.390625 :: 5.5

Then, as before directed, multiply the second and third Numbers, and divide by the first, and the quotient exhibits the fourth Proportional or the Number sought.

12.5

# *The Golden Rule.*

37

$$12.5 \cdot 5.390625 :: 5.5$$

$$\begin{array}{r} 26953125 \\ 26953125 \\ \hline \end{array}$$

$$12.5 \cdot 29.6484375 (2.371875$$

$$\begin{array}{r} 464 \\ 898 \\ \hline \end{array}$$

$$234$$

$$1093$$

$$937$$

$$625$$

$$00$$

*The Answer is 2 l. 7 s. 5 d. 1 q.*

**Quest. 2.** *If 6 Yards of Broad Cloth cost 4 l. what shall 32 Yards cost?*

Here the Term which asketh the Question is greater than the Term of like denomination, and requires more; therefore the Term of like denomination to the Term that asketh the Question is the Divisor.

$$6 \cdot 4 :: 32$$

$$4$$

$$\begin{array}{r} 128 \\ \hline \end{array}$$

6)

$$6)128(21.333$$

20

20

20

2

*The Answer is 21 l. 6 s.  $\frac{1}{3}$  d.*

*Quest. 3. If 320 Men raise a Breast-work in 6 Hours, in what time will 750 Men do the same?*

Here the Term that asketh the Question is more than the Term of like-denomination, and requires less; therefore the Term that asketh the Question is the Divisor, and this is the *Backer Rule of Three.*

$$320 . 6 :: 750$$

6

$$750)1920(2.56$$

4200

4500

00

*The Answer is 2 Hours, 33 Minutes, and 36 Seconds.*

*Quest.*



Quest. 4. If 756 Men dig a Trench in 12 Hours, in how many Hours will 126 dig the same?

Here the Term that asketh the question is less than the Term of like denomination, and requires more; then according to the Rule the Term demanding is the Divisor, and this question is also in the *Inverse Rule of Three*.

$$\begin{array}{r}
 756 \cdot 12 :: 126 \\
 \hline
 12 \\
 \hline
 126 \overline{) 9072} ( 72 \\
 \underline{252} \\
 00
 \end{array}$$

*The Answer is 72 Hours.*

There is sometimes four Numbers given in a question, yet is it but a *Single Rule of Three*, for one of the four Numbers is of no signification, and might as well have been left out.

*Example.*

Quest. 5. If 10 Workmen build a Wall 40 Foot long in 3 Days, in what time might 50 Men have done the same?

Here note, there is four numbers given, and yet there is but three to be used in working the

the question, you must therefore find which those 3 are that are necessarily to be used: Thus,

First, you must take the Term that asketh the question, here 50 Workmen; secondly, you must have the Term of like denomination with it, which is 10 Workmen; thirdly, the Term sought, being Days; you must take the Term of like denomination with that also, which is here 3 Days: The superfluous Term then in the question is 40, which might have been left out, and they will then stand thus:

$$\begin{array}{r} 10 \cdot 3 :: 50 \\ 3 \\ \hline 50 \cdot 30 \cdot 0 \cdot 5 \end{array}$$

*The Answer is Half a Day or 12 Hours.*

This question is in the *Rule of Three Inverse*.

Quest. 6. If 100 l. gain 6 l. in 12 Months, what shall 32 l. gain in the same time?

In this question the 12 Months is the superfluous Term, being of no use in the Calculation, the Terms required being 100 l. 6 l. and 32 l.

Note, Though the Terms in this question be all Money, and so may seem to be of one species, yet they are not; 100 l. and 32 l. are

## The Double Golden Rule. 61

are of one kind, being both Principal, and the other Term is of the same denomination with the Term sought, viz. Gain or Interest.

$$100 . 6 :: 32$$

6

$$100 \overline{) 192} ( 1.92$$

*The Answer is 1 l. 18 s. 4 d. 3 q. ferè.*

And this question is in the *Direct Rule of Three*, the Term that asked the question being less than the Term of like denomination, and also requiring less, &c.

## THE DOUBLE GOLDEN RULE.

**T**His Rule is called the *Double Golden Rule*, or *Double Rule of Three*, because it requires two distinct Calculations, before you can answer the question.

And in this Rule there are five Numbers given to find a sixth sought.

This differs not in the operation from the *Single Rule*, only the Calculation is twice repeated.

Of the five Numbers given, the question is sometimes annexed to two, and sometimes but to one.

If

If the question be annexed to two of the five given Numbers, then are there two of the other three of the same *species* with those that ask the question, and the third is proportional to the Number sought.

For the due regulation of these two Calculations, when the question is annexed to two of the five Numbers, take these Directions.

First, take one of the Numbers demanding; and let that ask the question in the first operation; secondly, take that of the same *species*, and also that of the like quality with the respondent, of these three constitute your first Rule of Proportion; then find which is your Divisor, according to your Rule *pag. 55.* and proceed to find the fourth in proportion.

Then for your second *Rule of Three*, take the other of the two Numbers to which the question is annexed, and let that ask the question; take also the Number of like kind, and the fourth Number found in the first Calculation; judge which is your Divisor, and work accordingly; the last Quotient will be the sixth Number, or the Number sought.

*Example.*

*If a Trench be 20 Perches in length, and made by 12 Men in 18 Days; how long may that Trench be, that shall be wrought by 48 Men in 72 Days?*

Here

*The Double Golden Rule.*

63

Here the question is annexed to two of the five Numbers, viz. 48 Men and 72 Days; now according to the foregoing direction, take one of the two Numbers inquiring, 48, and say,

*Men. Poles.*

$$\text{As } 12 \cdot 20 :: 48$$

20

$$12 \overline{) 960} \text{ ( 80 the fourth Number sought.}$$

Then take the other of the two Numbers inquiring, and say,

*Days. Poles.*

$$\text{As } 18 \cdot 80 :: 72$$

80

$$18 \overline{) 5760} \text{ ( 320 the sixth Number, and answer of the question.}$$

*If 6 Lighters bring 60 Tuns of Ballast in 5 Tides, how many Tun will 15 bring in 12?*

$$6 \cdot 60 :: 15 \cdot 150$$

$$5 \cdot 150 :: 12 \cdot 360 \text{ the sixth Number sought.}$$

*If*

If a Man travel 160 Miles in 4 Days, when the Days are 10 Hours long ; in how many Days will he travel 195 Miles , when the Days are 14 Hours long ?

$$160 . 4 :: 195$$

4

$$160 ) 780 ( 4.875 \text{ the 4th number.}$$

1400

1200

800

0

$$10 : 4.875 : 14$$

10

$$14 ) 48.75 ( 3.48214 \text{ the sixt number, and}$$

67

answer to the question, viz.

115

3 Days, 11 Hours, 34

30

Minutes, ferè.

20

60

4

When a Question is stated in the *Double Rule of Three* , so that there is but one Number inquiring,

First, take that Number ; and let it ask the question in the first Rule ; take also the Number of

of like denomination, together with the Number joyn'd to that of like denomination; and of these three Numbers constitute your first Rule of Proportion.

Secondly, let that Number which was found in the first Operation, ask the question in the second; then take the Number of like denomination to it, and also the Number joyn'd with that like Number; of these three is your second compounded; find your Divisor, and proceed; the last quote exhibits the Answer.

*Example.*

*If 4 Crowns at London make 2 Ducates at Venice, and 8 Ducates at Venice make 20 Pataccoons at Genoa; how many Pataccoons at Genoa will make 120 Crowns at London?*

Cr. Duc. Cr. Duc.  
First 4 . 2 :: 120 . 60

Duc. Pat. Duc. Pat.  
Second 8 . 20 :: 60 . 150

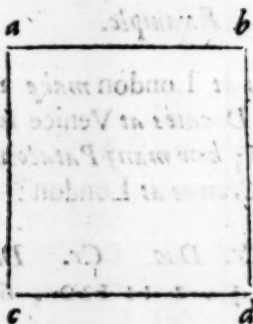




## Of the Square Root.

---

**A** Square is a plain Superficies bounded with four right Lines of equal length, the Angles also are equal, being all right Angles, as (*abcd*)



The measure of a Square is by a Square, that is, when it is known how many Square Inches, Feet or Perches, is contain'd in any Superficies, the Content or Area of the said Superficies is then said to be known. And in a Square, it is found by multiplying the length by the breadth, which being equal, it is called *Squaring of a Number*, and by the Learned Dr. Pell, *Involution*, and the Product or Area is the second Power; now the Side of such

such a Square is by Geometricians called a Root or the first Power.

Let the Side a b be 222 Inches, Feet, or Perches, &c.

222

444

444

444

49284 the Area or q. Number.

Now having the Area of a Square or Square Number given, and the Side or Root be required.

This is called the *Extraction of a Square Root*, and also *Evolution of the second Power*.

Let the Number be as before 349284.

The first thing to be done in the Extraction of a Root is punctation, or pointing the Number given; which is thus done, first set a point over the Unite-place, and omitting one point every other Figure thus, 349284; there being three points in the Number, intimates three figures in the Root

To proceed then, enquire the greatest Square Number contained in those figures, under the first point on the left hand; the greatest Square Number in 34 is 25, whose Root is 5, which place in the quotient for the first figure in the Root, subduct its Square out of 34, and set the Remainder 9 underneath as in the Example.

F 2

Ex.

Example.

$$\begin{array}{r}
 34 \overline{) 284} \text{ ( } 5 \\
 25 \phantom{00} \\
 \hline
 9
 \end{array}$$

The first figure in the Root thus found, the rest are found by Division; for a Dividend bring down the figures under the next point, and postpone them to the last Remainder, and the Example will stand thus, your Divisor being double the Root found.

$$\begin{array}{r}
 349 \overline{) 284} \text{ ( } 59 \\
 25 \phantom{00} \\
 \hline
 10 \overline{) 992} \\
 981 \phantom{00} \\
 \hline
 11
 \end{array}$$

Then I proceed to Division, always supposing the last Figure in my Divisor standing under the last save one in the Dividend; the Number to be subtracted from the Dividend must always be the Square of the last Figure in the Root, and the Divisor multiplied by the last Figure in the Root, so added together as in this Example, viz. so that the Unite-place in the last Number stand one place further to the right hand.

$$\begin{array}{r}
 \text{Nine times the Divisor} \text{ --- } 90 \\
 \text{And 9 multiplied by it self} \text{ --- } 81 \\
 \hline
 981
 \end{array}$$

Which

# Of the Square Root.

69

Which being subducted from the Dividend will remain 11, as part of a new Dividend, to them bring down the two next figures, and the Example will stand thus :

$$\begin{array}{r} 349284(59 \\ 25 \\ \hline 10)992 \\ 981 \\ \hline 118)1184 \end{array}$$

The Divisor as before is double the whole Root found, and for the Number to be subducted, after you have made enquiry how many times the Divisor will be found in the Dividend, if so placed as aforesaid, it will here be found once, then place 1 in the quotient for the third figure in the Root, the Number to be subducted will be as before, and the Example will stand thus :

$$\begin{array}{r} 349284(591 \\ 25 \\ \hline 10)992 \\ 981 \\ \hline 118)1184 \end{array}$$

The Divisor multiplied by the last Figure found, and the Square of that Figure placed as before directed.

F 3

Rest-

Rectangle ————— 118 .

Square ————— 1

1181

1181 subtracted from the Dividend 1184

There will remain but ————— 3

Which sheweth the Number was not a Square Number; but if you desire to have it further, add two Cyphers to the Remainder for a new Dividend, double your whole quotient for a new Divisor, and you may have as many Decimals as you please.

Tabula

*Tabula Laterum Quadra-  
torum ab Unitate ad 200.*

<i>Qua- drata.</i>	<i>Latera.</i>
1	1,000000,000000
2	1,41421,356237
3	1,73205,080757
4	2,000000,000000
5	2,23606,797750
6	2,44948,974278
7	2,64575,131106
8	2,82842,712474
9	3,000000,000000
10	3,16227,766017
11	3,31662,479036
12	3,46410,161514
13	3,60555,127546
14	3,74165,738677
15	3,87298,334621
16	4,000000,000000
17	4,12310,562562
18	4,24264,068712

<i>Qua- drata.</i>	<i>Latera.</i>
19	4,35889,894354
20	4,47213,595500
21	4,58257,569496
22	4,69041,575982
23	4,79583,152331
24	4,89897,948556
25	5,00000,000000
26	5,09901,951359
27	5,19615,242271
28	5,29150,262213
29	5,38516,480713
30	5,47722,557505
31	5,56776,436283
32	5,65685,424948
33	5,74456,264654
34	5,83095,189485
35	5,91607,978310
36	6,00000,000000
37	6,08276,253030
38	6,16441,400297
39	6,24499,799840
40	6,32455,532034
41	6,40312,423743
42	6,48074,069841



<i>Qua- drata.</i>	<i>Latera.</i>
43	6,55743,852430
44	6,63324,958071
45	6,70820,393250
46	6,78232,998313
47	6,85565,460040
48	6,92820,323028
49	7,00000,000000
50	7,07106,781185
51	7,14142,842854
52	7,21110,255093
53	7,28010,988928
54	7,34846,922835
55	7,41619,848710
56	7,48331,477355
57	7,54983,443527
58	7,61577,310586
59	7,68114,574787
60	7,74596,669241
61	7,81024,967591
62	7,87400,787401
63	7,93725,393319
64	8,00000,000000
65	8,06225,774830
66	8,12403,840464

<i>Qua- drata.</i>	<i>Latera.</i>
67	8,18535,277187
68	8,24621,125124
69	8,30662,386292
70	8,36660,026534
71	8,42614,977318
72	8,48528,137424
73	8,54400,374532
74	8,60232,526704
75	8,66025,403784
76	8,71779,788708
77	8,77496,438739
78	8,83176,086633
79	8,88819,441732
80	8,94427,191000
81	9,00000,000000
82	9,05538,513814
83	9,11043,357914
84	9,16515,138991
85	9,21954,445729
86	9,27361,849550
87	9,32737,905309
88	9,38083,151965
89	9,43398,113206
90	9,48683,298050

<i>Qua- drata.</i>	<i>Latera.</i>
91	9,53939,201417
92	9,59166,304663
93	9,64365,076099
94	9,69535,971483
95	9,74679,434481
96	9,79795,897113
97	9,84885,780180
98	9,89949,493661
99	9,94987,437107
100	10,00000,000000
101	10,04987,562112
102	10,09950,493836
103	10,14889,156509
104	10,19803,902719
105	10,24695,076596
106	10,29563,014099
107	10,34408,043279
108	10,39230,484541
109	10,44030,650891
110	10,48808,848170
111	10,53565,375285
112	10,58300,524426
113	10,63014,581273
114	10,67707,825203

<i>Quadrata.</i>	<i>Latera.</i>
115	10,72380,529476
116	10,77032,961427
117	10,81665,382639
118	10,86278,049120
119	10,90871,211464
120	10,95445,115010
121	11,00000,000000
122	11,04536,101719
123	11,09053,650641
124	11,13552,872566
125	11,18033,988750
126	11,22497,216032
127	11,26942,766958
128	11,31370,849898
129	11,35781,669160
130	11,40175,425099
131	11,44552,314226
132	11,48912,529308
133	11,53256,259467
134	11,57583,690279
135	11,61895,003862
136	11,66190,378969
137	11,70469,991072
138	11,74734,012447

<i>Qua- drata.</i>	<i>Latera.</i>
139	11,78982,612255
140	11,83215,956620
141	11,87434,208704
142	11,91637,528781
143	11,95826,074310
144	12,00000,000000
145	12,04159,457879
146	12,08304,597359
147	12,12435,565298
148	12,16552,506060
149	12,20655,561573
150	12,24744,871392
151	12,28820,572744
152	12,32882,800594
153	12,36931,687685
154	12,40967,364599
155	12,44989,959799
156	12,48999,599680
157	12,52996,408614
158	12,56980,508998
159	12,60952,021292
160	12,64911,064067
161	12,68857,754045
162	12,72792,206136

<i>Qua- drata.</i>	<i>Latera.</i>
163	12,76714,533480
164	12,80624,847487
165	12,84523,257867
166	12,88409,872673
167	12,92284,798332
168	12,96148,139682
169	13,00000,000000
170	13,03840,481041
171	13,07669,683062
172	13,11487,704860
173	13,15294,643797
174	13,19090,595827
175	13,22875,655532
176	13,26649,916142
177	13,30413,469565
178	13,34166,406413
179	13,37908,816026
180	13,41640,786500
181	13,45362,404707
182	13,49073,756323
183	13,52774,925847
184	13,56465,996625
185	13,60147,050874
186	13,63818,169699

<i>Qua- drata.</i>	<i>Latera.</i>
187	13,67479,433118
188	13,71130,920080
189	13,74772,708488
190	13,78404,875209
191	13,82027,496109
192	13,85640,646056
193	13,89244,398945
194	13,92838,827718
195	13,96424,004377
196	14,00000,000000
197	14,03566,884762
198	14,07124,727947
199	14,10673,597967
200	14,14213,562373

The Use of the precedent Table is principally for the ease of the industrious Artist; when he hath the Extraction of a Square Root in the Solution of any Question, it is but seeking the given Number in the Table, and just against it he shall find the Root. By the  
 Succedent



subsequent Examples will it plainly appear, how useful such a Table to 1000 Roots would be in quadratique Equations, and in the Cubes also, which (were there encouragement given to the Sons of Art) I doubt not but some ingenious Person would enrich the World therewith; these being long since Calculated by Mr. Henry Briggs of Oxford, and given me by my honoured Friend, Mr. John Collins, his desire being to have them made more publick, and the conveniency of such a Table (before mentioned) shewn, by some Examples upon this.

### Of Quadratique Equations.

Mr. Dary, in his *Miscellanies*, chap. 8. saith to this, or the like purpose:

1. When any Equation propos'd is incumbered with *Vulgar Fractions*, let it be reduced to its least Terms in whole Numbers, if possible; if not, let it be brought to its least Terms in Decimals.

2. It is evident from divers Authors, That if any Quantity shall be signed —, then the Square Root, or the Root of any even Power of such Quantity so sign'd, is inexplicable, for they cannot be generated from any Binomials that shall be equal.

As for Example.

— 9 being a Negative can be made of nothing (if taken as a Square Number) but  $-\sqrt{9}$  and

and — 3, which Roots are not equal, they being neither both Affirmatives nor both Negatives.

3. When you have cleared the Equation by the Second hereof, and that the Co-efficient in the highest Power is taken away, or be Unity, then will quadratigue Equations resolve themselves into the four following Compendiums.

4. Let your Equation be so reduced, that the highest Power stand on the left side alone, the sign + being always annexed, or supposed to be annexed.

Example, *Quesita a.*

First Equation.

$$\begin{array}{r}
 -\frac{1}{2}aa = -\frac{1}{2}ba + r \\
 \hline
 -\frac{1}{2}b - \sqrt{-\frac{1}{4}bb} + r = -\frac{1}{2}a \\
 -\frac{1}{2}b - \sqrt{-\frac{1}{4}bb} + r = -\frac{1}{2}a \\
 \hline
 -\frac{1}{4}bb + \sqrt{\phantom{x}}
 \end{array}$$

Second Equation.

$$\begin{array}{r}
 -\frac{1}{2}aa = -\frac{1}{2}ba - r \\
 \hline
 -\frac{1}{2}b - \sqrt{\frac{1}{4}bb} - r = -\frac{1}{2}a \\
 -\frac{1}{2}b - \sqrt{\frac{1}{4}bb} - r = -\frac{1}{2}a \\
 \hline
 -\frac{1}{4}bb - r
 \end{array}$$

G

Third

## Third Equation.

$$+aa = -ba + r$$


---

$$-\frac{1}{2}b + \sqrt{+\frac{1}{4}bb + r} = +a$$

$$-\frac{1}{2}b - \sqrt{+\frac{1}{4}bb + r} = -a$$


---

$$+\frac{1}{4}bb + r$$

## Fourth Equation.]

$$+aa = -ba - r$$


---

$$-\frac{1}{2}b + \sqrt{+\frac{1}{4}bb - r} = -a$$

$$-\frac{1}{2}b - \sqrt{+\frac{1}{4}bb - r} = -a$$


---

$$+\frac{1}{4}bb - r$$


---

*Illustration by Numbers, Quesita a.*

## First Equation.

$$+aa = +6a + 27$$


---

$$+3 + \sqrt{36} = -a \text{ And } a = +9$$

$$+3 - \sqrt{36} = -a \text{ And } a = -3$$


---

$$+9$$

$$+27$$


---

$$36$$

Proof

# *Of the Square Root.*

83

*Proof of the Affirmative.*

The Square of 9 = 81

Six times the Root = 54

To which add 27

81

Which was to be proved.

*Proof of the Negative.*

—3

—3

—3

+6

+9

—18

+27

+9

*Example 2.*

+aa = +8a + 46

+4 + √ + 62 = 7.874

4

+11.874 = +a

+4 — √ + 62 = —7.874

+4

+16

—3.874 = a

+46

+62

G 2

Second

## Second Equation.

## Example 1.

$$\begin{array}{r}
 +aa = +18a - 17 \\
 \hline
 +9 + \sqrt{+64} + 8 \\
 \hline
 +9 \\
 \hline
 +17 = a \\
 \\
 +9 - \sqrt{+64} + 8 \\
 \hline
 +81 \qquad \qquad \qquad +9 \\
 -17 \qquad \qquad \qquad \hline
 +1 = a \\
 \hline
 +64
 \end{array}$$

## Example 2.

$$\begin{array}{r}
 +aa = +14a - 46 \\
 \hline
 +7 + \sqrt{+3} = 1.73205, 080757 \\
 \hline
 7 \\
 \hline
 8.732 < = a \\
 \\
 +7 - \sqrt{+3} = 1.732 \\
 \hline
 7 \\
 \hline
 +49 \qquad \qquad \qquad 5.268 > = a. \\
 -46 \\
 \hline
 +3
 \end{array}$$

Third

Third Equation.

Example 1.

$$\begin{array}{r}
 +aa = -12a + 108 \\
 \hline
 -6 - \sqrt{+144} = +12 \\
 \hline
 \phantom{-6 - \sqrt{+144} = } -6 \\
 \hline
 \phantom{-6 - \sqrt{+144} = } +6 = a \\
 \hline
 -6 - \sqrt{+144} = -12 \\
 \hline
 \phantom{-6 - \sqrt{+144} = } -6 \\
 \hline
 +36 \\
 +108 \\
 \hline
 144
 \end{array}$$

Example 2.

$$\begin{array}{r}
 +aa = -20a + 94 \\
 \hline
 -10 + \sqrt{+194} = +13.92838,827718 \\
 \hline
 \phantom{-10 + \sqrt{+194} = } -10 \\
 \hline
 \phantom{-10 + \sqrt{+194} = } +3.92838,827718 = a \\
 \hline
 -10 - \sqrt{+194} = -13.9284 > \\
 \hline
 \phantom{-10 - \sqrt{+194} = } -10 \\
 \hline
 100 \\
 94 \\
 \hline
 194
 \end{array}$$

G 3

Fourth

## Fourth Equation.

Example 1.

$$\begin{array}{r}
 +aa = -10a - 9 \\
 \hline
 -5 + \sqrt{+16} = +4 \\
 \hline
 -5 \\
 \hline
 -1 = a \\
 \hline
 -5 - \sqrt{+16} = -4 \\
 \hline
 -5 \\
 \hline
 -9 = a \\
 \hline
 +25 \\
 -9 \\
 \hline
 +16
 \end{array}$$

Example 2.

$$\begin{array}{r}
 +aa = -16a - 36 \\
 \hline
 -8 + \sqrt{+28} = +5.29150,262213 \\
 \hline
 -8 \\
 \hline
 -2.70849,737787 \\
 \hline
 = a \\
 -8 - \sqrt{+28} = -5.2915 < \\
 \hline
 -8 \\
 \hline
 +64 \\
 -36 \\
 \hline
 +28 \\
 \hline
 -13.2915 < = a
 \end{array}$$

But



But if in a Square Equation there happen to be a Coefficient annexed to the highest Power, it is resolved by transferring the Coefficient with the Sign of Multiplication to the other side.

Admitting the Equation be

$$2aa = +6a + 8$$

Then the Coefficient 2 being transferred (as before directed) they will stand as in this Example.

*First Equation.*

$$2aa = +6a + 8 \times 2$$

$$+3 + \sqrt{25} = +2a$$

$$+3 - \sqrt{25} = -2a$$

$$+9$$

$$-16$$

$$+25$$

The Root of  $+25$  being  $+5$ , then is  $+5 + 3 = 8$ , and  $a = +4$ , the Affirmative Answer. And  $+3 - 5$  is  $-2$ , and  $a = -1$ , the Negative Answer.

The Proof is easie:

First, if  $a$  be  $= 4$ ,  $2aa$  is  $= +32$ , and  $6a$  is  $= +24$ , to which  $+8$  being added, the Sum is  $+32$  which was to be proved.

Again,  $a = -1$ , then  $2aa$  is  $= -2$ , whereto  $+8$  being added, the Sum is  $= +6$ , which also was to be done.

## Second Equation.

$$4aa = +26a - 12 \times 4$$

$$+13 + \sqrt{121} = +4a$$

$$+13 - \sqrt{121} = +4a$$

$$\begin{array}{r} 39 \\ 13 \\ \hline \end{array}$$

$$\begin{array}{r} +169 \\ -48 \\ \hline \end{array}$$

$$121$$

Now  $+13 +$  the  $\sqrt{121}$ , viz.  $+11$  is  $=+24$ , the  $\frac{1}{4}$  whereof is  $=+6=a$ , and  $aa=36$ , and  $4aa=+144$ ,  $+26a=+156$ , to which if  $-12$  be added, the Sum will be  $+144$  also.

Again, If to  $+13$  you add  $-$  the  $\sqrt{121}$ , viz.  $-11$ ,  $4a$  will be  $=+2$ , and consequently  $+a=+\frac{1}{2}$ ,  $4aa$  is then  $=+1$ , and  $+26=+13$ , to which add  $-12$ , and the Sum is  $=+1$ , which was to be proved.

## Third Equation.

$$5aa = -6a - 32 \times 5$$

$$-3 + \sqrt{169} = +5a$$

$$-3 - \sqrt{169} = +5a$$

$$\begin{array}{r} +9 \\ +160 \\ \hline \end{array}$$

$$+169$$

$-3 - 13 = -15a$ , here  $a = -2$ ,  $5aa = +20$ ,  $-6a = -12$ , to which add  $+32$ , the Sum is also  $+20$ .

Again,  $-3 - 13 = -16 = -5a$ , and  $a = -3.2$ ,  $5aa = +51.2$ : Also  $-6a$  being  $+19.2$ , to which add  $+32$ , the Sum is  $+51.2$ .

Fourth Equation.

$$2aa = -10a - 8 \times 2$$

$$-5 + \sqrt{9} = -2a$$

$$-5 - \sqrt{9} = -2a$$

$$+25$$

$$-16$$

$$+9$$

$$-5 + 3 = -2a, \text{ then } a = -1, -10a = +10$$

$$-8$$

$$2aa = +2$$

$$+2$$

$$-5a - 3 = -2a, \text{ then is } a = -4$$

$$-10$$

$$-a = -4$$

$$+40$$

$$-4$$

$$-8$$

$$+16$$

$$+32$$

$$2$$

$$+32$$

Which was to be done.

Note,

—*Note*, Always where there is no Sign annexed to any Term in the Equation, the Sign  $+$  is supposed to be annexed.

I have been the larger in these Examples, that the young *Analist* may with the more ease apprehend the several kinds by this variety; in some of the furd Roots I have on purpose omitted the large number of Places, four or five being sufficient for use in most cases; but if any desire to be more exact, he may take them as far as he pleaseth, or the Table doth exhibit.

---

of

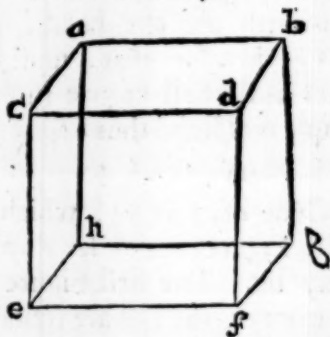
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## Of the Cube Root.

**T**He Cube is a Solid, and hath three dimensions, length, breadth, and depth, and is inclosed by six plain square Superficies.

*Example.*



Let the Side *a, b, or c, d, &c.* be 125: To find the Content in Solid Feet or Inches, is the Involution of the Side or Root. Thus:

125	15625
125	125
—	—
625	78125
250	31250
125	15625
—	—
15625	1953125 The Solidity.
And this is called the Third Power.	The

The Evolution hereof, is also termed the Extraction of the Cube Root, wherein observe first your punctation, omitting two, point every third Figure.

*Example.*

71953125

The first Figure in the Root is found by taking the greatest Cube Number, contained in the Figure or Figures that stand under the first Point towards the left hand, here 71, whose Root is 4, therefore that 4 must be placed in the Quotient as the first Figure in the Root, and the Example will stand thus;

71953125 ( 4

Then the Cube of 4 is 64, which subduct out of the first Figures, and set down the remainder if any be. The first Figure found in this peculiar manner, the rest are found by Division thus: The Dividend consists of the remainder, if any be, and the three Figures under the next Point postponed; the Divisor is always three times the Square of the Root, and three times the Root it self: These two Numbers being so to be added together, as that the Unites of the first stand over the Tens of the second.

Three times the q. of the  $\sqrt{= 48}$

Three times the  $\sqrt{= 12}$

---

Divisor 492

Then

Then will the Example stand thus :

$$\begin{array}{r} 71953125 \text{ ( 4} \\ 64 \\ \hline \end{array}$$

$$492 \text{ ) } 7953$$

Then proceed to Division, always supposing the last Figure in the Divisor to stand under the last save one in the Dividend, and enquire, how many times 4 in 7? place 1 in the Quotient. Then for your Number to be subducted out of the Dividend, it always consists of three Numbers, viz.

Three times the q. of the first Figure = 48

Multiplied by the second 1

Product of the first by the second 48

3 times the q. of the second by the first 12

And the Cube of the second 1

The Subducend 4921

$$\begin{array}{r} 71953125 \text{ ( 41} \\ 64 \\ \hline \end{array}$$

$$\begin{array}{r} 492 \text{ ) } 7953 \\ 4921 \\ \hline \end{array}$$

The q. of 41 = 1681

3

3032

q of 41  $\times$  3 = 5043

Then for a new Dividend, bring down the three next Figures, postponing them as before.

The Divisor thrice the q. of the  $\sqrt{41} = 5043$

And three times the  $\sqrt{41} = 123$

50553

Which



Which being set on the left hand the Dividend, stands thus :

$$\begin{array}{r}
 71953125(415 \\
 64 \\
 \hline
 492(7953 \\
 4921 \\
 \hline
 50553)3032125
 \end{array}$$

Then enquire, how many times 5 in 30? you will find 5 times, which place in the Quotient. Your Subducend is as before,

$$\begin{array}{r}
 3 \text{ times the Square of } 41 \times 5 = 25215 \\
 3 \text{ times the Square of } 5 \times 41 = 3075 \\
 \text{And the Cube of } 5 = 125
 \end{array}$$

$$\begin{array}{r}
 \text{The Subducend } 2552375 \\
 \text{Which being subducted from } 3032125 \\
 \hline
 \end{array}$$

$$\text{There will remain } 479750$$

Which shews the Number was not a Cube Number; if you add three Cyphers, and work as before, you may have as many Decimals Fractions as you please.

In this Extraction I have not taken the same Number the Cube first mentioned did produce, but by adding another Figure, made the Number greater, that it might take in all Cases; but in the following Extraction it is explicated.

$$1953125$$

*Of the Cube Root.*

95

1953125 (125

1

33 ) 0953

728

4356 ) 225125

225125

0

Three times the Square of the Root = 3

Three times the Root is also = 3

The first Divisor = 33

Three times the Square of 1 = 3

2

Three times the Square of  $1 \times 2 = 6$

Three times the Square of  $2 \times 1 = 12$

The Cube of 2 = 8

The first Subducend = 728

12

12

144

3

Three times the Square of the Root = 432

Three times the Root = 36

The second Divisor = 4356  
Three

Three times the Square of the  $\sqrt{12} = 432$   
5

---

Three times the Square of  $12 \times 5 = 2160$

Three times the Square of  $5 \times 12 = 900$

The Cube of 5 = 125

---

The second Subducend = 225125

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A

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A SHORT  
TREATISE  
OF  
SIMPLE & COMPOUND  
INTEREST:  
WITH  
TWO TABLES  
FOR THE  
CALCULATION  
OF

The Value of *Leases* or *Annuities* by  
Quarterly Payments, at 6 per Cent.  
*per Annum.*

---

By *John Mayne.*

---

*London*, Printed by *William Godbid*, for  
*Nath. Crowch*, in *Exchange-Alley*.

M. DC. LXXIII.

A SHORT  
TREATISE  
OF  
SIMPLE & COMPOUND  
INTEREST  
WITH  
TWO TABLES  
FOR THE  
CALCULATION

OF  
The Value of Reversions or Annuities by  
Quarterly Payments at 4 per Cent.  
per Annum.

---

By John Mayne.

---

London, Printed by William Gellish, for  
J. B. Crocker, in Strand, 1751.  
M. D. C. LXXI.



## Of Simple Interest.

**Q**uestions in *Simple Interest* are wrought by the Double Rule of Proportion, wherein five Numbers are given to find the six.

And if you put  $P = 100$  Principal, and  $T$  for Twelve Months,  $G = 6$  l. the Rate of Interest, and  $p =$  any other Sum greater or lesser,  $t =$  any other Time (above or under Twelve Months) and also  $g =$  the Gain thereof at that Rate.

Then if any one Term of these six be unknown, it is explicated by the other five (like Symbols having the same denomination) as in this Equation.

$$P T g = p t G$$

That is the Fact of 100 l. multiplied by one year, and that Product by 6 the Interest of 25 l. for 4 years, is equal to the Fact of 25 multiplied by 4 years, and that Product by 6 the Interest of 100 l. for one year.

Example.

$$\begin{array}{rcl}
 P = 100 & & p = 25 \\
 T = 1 & & t = 4 \\
 \hline
 g = 6 & & G = 6 \\
 \hline
 600 & & 600
 \end{array}$$

Which was to be proved.

Now forasmuch as the usual Questions of Simple Interest, are proposed from a Sum presently due to the Gain thereof, & *contra*; it will be requisite you put  $A =$  the Amount of a Sum, forborn or due hereafter, and then you will have  $A = p + g$ , as in the former Equation.

Example.

$$\begin{array}{rcl}
 P & T & P + G \\
 \text{As } 100 \text{ in } 1 \text{ to } 106 & & \\
 \text{So } 25 \text{ in } 4 \text{ to } 31 = p + g & &
 \end{array}$$

From the precedent Analogism will arise these four Propositions.

Prop. I.

A Sum presently due  $= p$ , being forborn a certain time  $= t$ , at a certain rate  $= G$ , per Cent per Annum: Q. the Amount  $= A$ ?

Equa-



$$\text{Equation } A = \frac{P \times G}{T \times P} + P.$$

That is, the given Sum multiplied by the given Time, and that Product again multiplied by the given Rate of Interest, the last Product divided by the Principal, viz. 100, in the Time, viz. 1, exhibits the Gain of that Sum in that Time.

## Illustration.

Quest. 1. 25 L. being forborn 18 Months, at 6 per Cent. per Annum; what doth it amount to?

$$25 = P$$

$$1.5 = T$$

$$\frac{125}{25}$$

$$25$$

$$P = 100$$

$$T = 1$$

$$37.5$$

$$6 = G$$

$$PT = 100 \times 225.0 \times 2.25$$

$$25 = P$$

$$27.25 = A$$

The Answer being 27 L. 5 s. the Amount in that time.

Quest. 2. If 175 L. be forborn for 7 Years, at 6 per Cent. per Annum, Simple Interest; what will it amount to at the end of the said time?

$$175 = p$$

$$7 = t$$

$$1225$$

$$6 = G$$

$$TP = 100) 73.50$$

$$175 = p$$

The Answer = 248.5 That is 248 l. 10 s.

Prop. II.

*A Sum of Money = A, due at a certain time hereafter = t, at a certain Rate of Interest = G, per Cent. per Annum. Q. The present worth = p?*

$$\text{Equation, } p = \frac{ATP}{TP + tG}$$

That is, the Fact of the Amount multiplied by the Principal, 100, in the Time, viz. 1 Year, divided by the said Principal multiplied into the said Time, more the Rate of Interest multiplied into the Time of Forbearance, the Quotient is equal to the present worth.

*Example.*

*Quest. I.* If 248 l. 10 s. be due at the end of 7 years, what is it worth in ready money, discounting Interest, at 6 per Cent. per Annum.

$$7 = t$$

# Of Simple Interest.

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$$\begin{array}{r} 7 \text{ = } t \times 9 \quad 248.5 \text{ = } A \\ 6 \text{ = } G \quad 100 \text{ = } P T \end{array}$$

$$\begin{array}{r} 42 \quad 142 \quad 24850.0 \quad (175 \text{ = } P \\ PT = 100 \quad 1065 \\ 142 \quad 710 \\ 60 \end{array}$$

The Answer is 175 l.

*Quest. 2. If 950 l. be due at the end of 12 years, what is it worth in ready money, at 9 per Cent. per Annum Simple Interest?*

$$\begin{array}{r} 12 \text{ = } t \quad 950 \text{ = } A \\ 9 \text{ = } G \quad 100 \text{ = } P T \\ 108 \text{ = } 208 \quad 95000 \quad (456.7307 \\ PT = 100 \quad 1180 \\ 1400 \\ 1520 \\ 640 \\ 1600 \\ 144 \end{array}$$

The Answer is 456 l. 14 s. 7 d.  $\frac{1}{4}$  ferè.

**Prop. III.** *A Sum presently due = p, having been forborn a time unknown = t, did amount to a certain Sum = A, at a Rate of Interest = G, per Cent. per Annum. Q. the Time of forbearance = t?*

H 4

Equa-

# Of Simple Interest.

$$\text{Equation, } \frac{A - p; \times TP}{pG} = t.$$

That is to say, the Amount less the Principal, so increased, multiplied by 100, and that Product divided by the Fact of the before-mentioned Principal, and Rate of Interest, quotes the Time of forbearance.

## Example.

Quest. 1. If 175 l. hath been forborn till with the Interest at 6 per Cent. per Annum it is increased to be 248 l. 10 s. Q. How long hath it been forborn?

$$\begin{array}{r} 175 = p \\ 248.5 = A \\ 6 = p \\ 175 = p \\ 1050 \\ 73.5 = A - p \\ 100 = P.T. \\ 1050 ) 7350.0 ( 7 = t \\ 0000 \end{array}$$

The Answer is 7 years.

Quest. 2. If 25 l. hath been forborn till it is amounted to 27 l. 5 s. at 6 per Cent. per Annum Simple Interest. Q. In what time is it so increased?

$$\begin{array}{r} 25 \\ 27.25 \end{array}$$

# Of Simple Interest.

105

$$A = 27.25$$

$$p = 0.125$$

$$q = 1$$

$$r = 1.25$$

$$25$$

$$A = 27.25$$

$$0.125$$

$$T = 100$$

$$0.125$$

$$2.25$$

$$0.125$$

$$100$$

$$0.125$$

$$2.25$$

$$0.125$$

$$150) 225.00 (1.5$$

$$750$$

$$00$$

The Answer 1 year and an half.

Prop. IV.

A Sum of Money = p, being forborn a certain time = t, and at the end of that Term did amount to a Sum = A. Q. At what Rate of Interest?

$$\text{Equation, } \frac{A - p : \times TP}{tp} = G.$$

Or from the Amount subduct the Principal, and the Remainder multiply by 100, that Product divided by the Principal multiplied by the Time, the Quotient will be = G the Rate of Interest, per Cent. per Annum.

Illustration.

Quest. 1. If 250 l. forborn 3 years and 6 months, did amount to 324 l. 7 s. 6 d. at what Rate of Interest did it so increase?

250

$$250 = p$$

$$3.5 = r$$

$$1250$$

$$750$$

$$875$$

$$324.375 = A$$

$$250 = p$$

$$74.375 = A - p$$

$$100 = TP$$

$$875 \div 7437.5 (8.5$$

The Answer is 8  $\text{l. } 10 \text{ s.}$

*Quest. 2.* If 175  $\text{l.}$  being forborn 7 years, did amount to 248  $\text{l. } 10 \text{ s.}$  what Rate of Simple Interest *per Cent. per Annum* was it accounted at?

$$175$$

$$7$$

$$1225$$

$$248.5$$

$$175$$

$$73.5$$

$$100$$

$$1225 \div 7350.0 (6 = G$$

$$0000$$

The Answer is 6  $\text{l.}$

If one month be taken for the  $\frac{1}{12}$  of a year, the business of Interest and Rebate is very easily performed by a small Table of the Amounts of 1  $\text{l.}$  for any number of months, not exceeding 12; which Table is made by this Analogy, 100.106::1.1.06.

*A Table of the Increase of  
1 l. at 6 per Cent per Ann.*

<i>Months.</i>	<i>Value.</i>	<i>Months.</i>	<i>Value.</i>
12	1.06	6	1.03
11	1.055	5	1.025
10	1.05	4	1.02
9	1.045	3	1.015
8	1.04	2	1.01
7	1.035	1	1.005

If the Question be of the Amount of any Sum forborn any number of months, at 6 per Cent. per Annum, multiply the given Sum by the Tabular Number for that time, and the Product answers the Question.

*Example.*

If 125 l. be forborn 10 months, what will it amount to?

The Principal = 125  
The Tabular Number for 10 months = 1.05

$$\begin{array}{r} 625 \\ 1250 \\ \hline \end{array}$$

131.25

The Answer is 131 l. 5 s.

If



If the Question be only what is the Interest of any Sum for any time, then multiply the Sum for that time by the Tabular Number less an Unite.

*Example.*

What is the Interest of 125 *l.* for 10 months?

$$\begin{array}{r} \text{The Principal} = 125 \\ \text{The Tabular Number less an Unite} = .05 \\ \hline 6.25 \end{array}$$

The Answer is 6 *l.* 5 *s.* *prout supra.*

For Discompt or Rebate of any Sum to be forborn, the present worth is found by dividing the given Sum by the Tabular Number.

*Example.*

What is the present worth of 131 *l.* 5 *s.* due at the end of 10 months?

$$1.05 \overline{) 131.25} \quad (125$$

$$262$$

$$525$$

$$0$$

The Answer is 125 *l.*

But if any desire to be more exact, let him multiply the Interest of 1 *l.* for 1 day (which is

is .000164384) by the number of days, and that Product by the given Sum, and the last Product will be the Interest for that Sum forborn the time given.

*Example.*

What is the Interest of 125 *l.* forborn from the Tenth of *March* to the Tenth of *January* following, viz. 305 days?

.000164384

305

821920

4931520

.050137120

125

25068560

10027424

5013712

6.26714000

The Answer is 6 *l.* 5 *s.* 4 *d.* fere.

Discompt is performed by Division, viz. get the Amount of 1 *l.* for the time required, by which divide the given Sum, and the Quote is the present worth.

## Of Mean Time.

It hath been a custome amongst Merchants, in their Contracts upon Sale of Commodities, to agree upon divers times of payment, as two three-months, three six-months, &c. Now to find a time between these, wherein the whole Sum may be paid at one entire Payment without detriment to either Party, the subsequent Table doth shew upon the first inspection.

A Table for Equation of Time.

2	1 is 1.5	3	1 is 2	4	1 is 2.5	5	1 is 3
	2 is 3		2 is 4		2 is 5		2 is 6
	3 is 4.5		3 is 6		3 is 7.5		3 is 9
	4 is 6		4 is 8		4 is 10		4 is 12
	5 is 7.5		5 is 10		5 is 12.5		5 is 15
	6 is 9		6 is 12		6 is 15		6 is 18
	7 is 10.5		7 is 14		7 is 17.5		7 is 21
	8 is 12		8 is 16		8 is 20		8 is 24
	9 is 13.5		9 is 18		9 is 22.5		9 is 27
6	1 is 3.5	7	1 is 4	8	1 is 4.5	9	1 is 5
	2 is 7		2 is 8		2 is 9		2 is 10
	3 is 10.5		3 is 12		3 is 13.5		3 is 15
	4 is 14		4 is 16		4 is 18		4 is 20
	5 is 17.5		5 is 20		5 is 22.5		5 is 25
	6 is 21		6 is 24		6 is 27		6 is 30
	7 is 24.5		7 is 28		7 is 31.5		7 is 35
	8 is 28		8 is 32		8 is 36		8 is 40
	9 is 31.5		9 is 36		9 is 40.5		9 is 45

The

## Of Simple Interest. 111

The manner of making this Table, is no more than adding one Term to the given number of Terms, and take half the Sum.

### Example.

Is three four-months given, add 4 to 12, the Sum will be 16, half that Sum, *viz.* 8 months, is the equated Time of Payment.

This indeed is but an approximation, though near enough the truth for practice. That excellent Accomptant Mr. Collins, in a Sheet Printed Anno 1665. hath taught a more exact way of Equation: *Simple Interest*, prop. 4. Compute (saith he) all the present worths, and then by proportion, if all those present worths amounted to the total of all those Payments, what did 1 l. amount to in the said time? From the result subtract an Unite, the Remainder is the Interest of 1 l. for the time sought, which divide by the Interest of 1 l. for one Day, and the Quote is the Number of Days sought.

### Example.

A Merchant sold Wines for 300 l. and hath given the Vintner three six-months for Payment, *viz.* to pay 100 l. at the end of 6 months, another at 12, and the third 100 l. at 18 months end, the Question is, At what time may this Vintner pay 300 l. together, without detriment to himself or the Merchant,

The number of making this Table, is no more than adding the given number of Terms, and the sum.

$$1.03) 100.0 (97.087$$

730

900

760

Is three four months given, add 4 to 12 the sum will be 16, that sum, with 2 months, is the required Time of Payment.

$$1.06) 100.0 (94.339$$

460

360

420

1020

66

The interest is but a small addition, though near enough the truth for practice. That which is a convenient Method, in a Short Printed Book, is a more exact way of proportion: divide the sum by the number of Terms, and then by the number of Terms, and the result is the present worth.

$$1.09) 100.0 (91.825$$

190

890

280

620

66

100 l. at 6 months is worth — 97.087

100 l. at 12 months is worth — 94.34

100 l. at 18 months is worth — 91.826

The present worths = 283.253

# Of Simple Interest:

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283.253 ) 300.00000 ( 1.059123786

1674700

2584350

350730

674770

1072640

2228810

2460390

1943660

240142

The Interest of 1 £. for the time is .059123786

The Interest of 1 £. for 1 day is = .000164384

.000164384 ) .059123786 ( 359.6

980858

1589346

19930

The Answer is 359 days and a half, *ferè*.

By the Table, three six-months gives twelve months for the equated time, which you find above five days less than a year by this Calculation.

*A Decimal Table of the present worth of One Pound, Quarterly Payment, at 6 per Cent. per Annum, Simple Interest, for 124 Quarters.*

1	.985222	21	18.136533
2	1.956095	22	18.888413
3	2.913033	23	19.631907
4	3.856429	24	20.367201
5	4.786662	25	21.094474
6	5.704093	26	21.813898
7	6.609071	27	22.525642
8	7.501928	28	23.229868
9	8.382985	29	23.926732
10	9.252550	30	24.616387
11	10.110919	31	25.298981
12	10.958377	32	25.974656
13	11.795197	33	26.643553
14	12.621643	34	27.305804
15	13.437970	35	27.961542
16	14.244421	36	28.610893
17	15.041234	37	29.253979
18	15.828636	38	29.890922
19	16.606846	39	30.521837
20	17.376077	40	31.146837



41	31.766032	66	45.627833
42	32.379529	67	46.125686
43	32.987432	68	46.621636
44	33.589841	69	47.113036
45	34.186856	70	47.600841
46	34.778572	71	48.085103
47	35.365082	72	48.565872
48	35.946478	73	49.043199
49	36.522847	74	49.517133
50	37.094275	75	49.987721
51	37.660848	76	50.455010
52	38.222645	77	50.919048
53	38.779748	78	51.379877
54	39.332235	79	51.837543
55	39.880180	80	52.292088
56	40.423658	81	52.743556
57	40.962742	82	53.191986
58	41.497501	83	53.637421
59	42.028005	84	54.079898
60	42.554321	85	54.519459
61	43.076514	86	54.956140
62	43.594649	87	55.389980
63	44.108787	88	55.821014
64	44.618992	89	56.249280
65	45.125321	90	56.674811

91	57.097644	111	65.035628
92	57.517813	112	65.408763
93	57.935349	113	65.779820
94	58.350287	114	66.148824
95	58.762658	115	66.515796
96	59.172494	116	66.880760
97	59.579826	117	67.243736
98	59.984684	118	67.604747
99	60.387099	119	67.963814
100	60.787099	120	68.320956
101	61.184713	121	68.676196
102	61.579970	122	69.029553
103	61.792897	123	69.381047
104	62.363522	124	69.730697
105	62.751872		
106	63.137972		
107	63.521849		
108	63.903529		
109	64.283035		
110	64.660394		

The Use of the precedent Table is principally to shew the present worth of any Lease or Annuity, payable Quarterly, for any term of years under 31, at 6 per Cent. per Annum Simple Interest.

Example

Example.

There is a Lease for 18 years to be sold, of the yearly value of 160 *l.* payable Quarterly, viz. 40 *l.* per Quarter, what is this Lease worth in ready money, allowing the Purchaser 6 per Cent. Simple Interest?

$$72 \text{ Quarters per Table} = 48.565872$$

$$1942.634880$$

The Answer is 1942 *l.* 12 *s.* 8 *d.*  $\frac{1}{4}$  ferè.

The Inversion of the Question, viz. What Quarterly Payment for 18 years will 1942 *l.* 12 *s.* 8 *d.*  $\frac{1}{4}$  purchase?

As the former was done by Multiplication; where the Product exhibits the Answer; so if the Sum proposed be divided by the Tabular Number, the Quote gives your Answer.

Example.

$$48.565872 \overline{) 1942.634880} \quad 40$$

0000 00000

The Answer is 40 *l.*



## Of Compound Interest.

**A**S Simple Interest is performed by a Series of Musical, so is Compound Interest wrought by a Rank of Geometrical continual Proportionals. The operation whereof by the Canon of Logarithms, take under these four Considerations.

### Prop. I.

*If you shall put  $p$  = the Logarithm of a Principal or Sum forborn, and  $t$  = the time of forbearance in years, quarters, months, or days,  $r$  = the Logarithm of the Rate of Interest, per cent. per annum, per mensem, or per diem,  $a$  = the Logarithm of the Amount of the said Principal for the said time, at the Rate also aforesaid: Then Q. The Amount =  $a$ ?*

Equation,  $a = r \cdot t + p$ .

That is, Multiply the Logarithm of the Rate by the Number of Years, Quarters, &c. to which Product add the Logarithm of the Principal, and the Aggregate is equal to the Logarithm of the Amount.

*Example.*

Example.

Quest. 1. If 175 l. be forborn 7 years, what will it amount to at 6 per Cent. per Annum, Compound Interest?

$$\text{Log. of the Rate} = 0,02530586 = r$$

$$7 = t$$

$$\hline 0,17714105$$

$$\text{Log. of the Sum} = 2,24303805 = 175 = p$$

$$\hline 2,42017910 = 263.135$$

The Answer 263 l. 2 s. 8 d.  $\frac{1}{4}$  ferè.

Quest. 2. If 1000 l. be forborn for 6 months, at 6 per Cent. per Annum, Compound Interest, what will it amount to?

$$\text{Log. of the former Rate divided by 12, the months in a year, is} = 0,00210882 = r$$

$$6 = t$$

$$\hline 0,01265292$$

$$\text{Add the Log. of 1000 viz. } 3,00000000$$

$$\hline 1029.563 = \text{Log. Amount } 3,01265292 = A$$

The Answer 1029 l. 11 s. 3 d. ferè.

## Prop. II.

*A Sum of Money unknown, being forborn a certain time = t, at a given Rate of Interest = r, is amounted to a given Sum = a;  
Q What was p?*

$$\text{Equation, } p = a - rt.$$

From the Logarithm of the Amount, subtract the Logarithm of the Rate, multiplied by the time, and the Remainder is the Logarithm of the Principal.

*Example.*

*Quest. 1. If 263 l. 2 s. 8 d.  $\frac{1}{4}$  be the Amount of a Sum forborn 7 years, at 6 per Cent. per Annum, Compound Interest, what was the Principal?*

$$\text{Log. of the Rate} = 0,02530586 = r$$

$$7 = t$$

---


$$0,17714105 = rt$$

$$\text{Log. of the Amount } 2,42017910$$

---


$$\text{Log. of the Principal } 2,24303805 = p = 175$$

The Answer 175 l.

*Quest.*

# Of Compound Interest. 121

*Quest. 2.* If 102 l. 11 s. 3 d. be the Principal and Interest of a Sum of Money forborn 6 months, at 6 per Cent. per Annum, Compound Interest, what was the Principal?

Log. of Rate for 1 m°. 0,00210882  
6

0,01265292  
Log. of 1029.563 = 3,01265292

Log. of the Principal 3,00000000 = 1000  
The Answer 1000 l.

## Prop. III.

*A Sum of Money = p, being forborn for a time = t, did amount to a given Sum = a, at a Rate of Interest unknown: Q. The Rate per Cent. per Annum = r?*

$$\text{Equation, } r = \frac{a - p}{t}$$

Divide the Logarithm of the Amount, less the Logarithm of the Principal, by the Time, and the Quote is the Logarithm of the Rate.

## Example.

If 25 l. forborn 4 years, did amount to 31 l. 11 s. 2 d.  $\frac{1}{4}$ ; at what Rate of Compound Interest did it so increase?

Loga-



122 *Of Compound Interest.*

Logarithm of the Amount = 1,49808345

Logarithm of the Principal = 1,39794001

$a - p$  divide by 4 ) 0,10014344

The Log. of the Rate =  $r = 0,02503586$

Prop. IV.

*A Sum of Money being forborn, at a given Rate, for a time unknown, but the Amount is known, how long was it so forborn?*

$$\text{Equation, } t = \frac{a - p}{r}.$$

*Example.*

If 1000 l. be increased to 1029 l. 11 s. 3 d. at 6 per Cent. per Annum, Compound Interest, in what time was it so increased?

$$r = 0,00210882 \quad a - p = 0,01265302(600000010$$

The Answer 6 months.

It may here be expected that I should lay down the Construction of the Logarithms, having made use of them in these Calculations, but this being design'd a small *Enchiridion*, and there being large Volumans of that Subject in the World already, by several more learned Pens, I think it unnecessary to say any thing further.

further thereof, for as they are of excellent use, so are they easie to be had.

---

**C**omound Interest *Infinite*, may be so called as it relates to divers equal Payments at equal times, but the number of those equal times are infinite, (*i. e.*) when an Estate in Fee-Simple shall be sold for ever. Now there being usually an interval of time, between the Purchasers Payment and the reception of his first Rent, be it yearly, half yearly, or quarterly;

*Any Question of this Nature may be wrought by the following Analogism:*

Putting  $V$  = the Rent (yearly or quarterly)  
 and  $S$  = the Price paid for the Land,  
 also  $R$  = the Common Factor of the  
 Rate of Interest, *per Cent. per Annum.*

Hence then may arise these three Propositions.

Prop. I.

*There is a Fee Simple to be sold, what is it worth in ready money, so that the Purchaser may have 6 per Cent. per Annum, Compound Interest, allowed for his money.*

*Quest.*

*Quest. 1.* There is a Manour to be sold of the clear yearly value of 969 *l.* 18 *s.* what Sum of ready money is this Estate worth, 6 *per Cent. per Annum* Compound Interest being allowed the Purchaser for his money?

$$\text{Equation, } \frac{V}{R-1} = S;$$

The Annual (or Quarterly) Payment, divided by the Ratio, less Unity, exhibits the Sum in the Quotient.

$$\begin{array}{r} R-1 = .06 ) 969.9 ( 16165 \\ \underline{36} \\ 09 \\ \underline{39} \\ 30 \\ \underline{30} \\ 0 \end{array}$$

The Answer is 16165.

*Quest. 2.* There is an Estate of 969 *l.* 18 *s.* *per Annum*, payable Quarterly, what is it worth in ready money, allowing the Purchaser 6 *per Cent. per Annum* Compound Interest?

# Of Compound Interest.

125

R—i V S

1014674) 242.475 (16524.124

14674

95735

88044

76910

73370

35400

29348

60520

58696

18240

14674

35660

29348

63120

58696

4424

The Answer is 16524 l. 2 s. 6 d. *ferè*.

The difference between Yearly and Quarterly Payments in this Purchase raiseth the value 359 l. 2 s. 6 d.

Having the increase of 1 l. for a Year, at any Rate of Interest, the Biquadrate Root of that Increase, is the Increase of 1 l. for a Quarter at Compound Interest.

Prop.

## Prop. II.

*A Sum of money lying ready for a Purchase; and it be desired to know what Free-hold Estate such a Sum will purchase, if laid out at a given Rate per C. per Ann. Compound Interest.*

Theorem,  $V = S \times R - 1$ .

Or, in other terms, the Sum of Money multiplied by the Rate, less Unity, the Product shall be equal to the Annual half quarterly or quarterly Payment.

*Quest.* A Gentleman upon Marriage of his Daughter promiseth to lay out 1600 l. for a Free-hold Estate, to be settled upon her and her Heirs, provided he meet with such a Pennyworth as shall bring 8 per Cent. per Annum, Compound Interest for his money: Q. What Annual Rent must it be?

$$\begin{array}{r} 1600 = S \\ .08 = R - 1 \end{array}$$

---


$$V = 128.00$$

The Answer 128 l. per Annum.

## Prop. III.

*An Estate being offered for a certain Sum of money, the annual Rent is also known: Q What Rate*

# Of Compound Interest. 127

Rate of Interest upon Interest shall the Purchaser have for his money?

$$\text{Equation, } \frac{V}{S} = R - 1.$$

The annual Rent being divided by the Sum demanded, quotes the Rate less Unity.

*Example.*

*Quest. 1.* There is a Free-hold Estate to be sold for 1600 l. the yearly Rent being 128 l. what Rate of Interest shall the Purchaser have for his money?

$$1600 ) 128.000 (.08 = R - 1.$$

Add 1.00

$$\hline 1.08 = R.$$

*Quest. 2.* Admit there be a small Farm to be sold of the Value of 35 l. per Annum for 500 l. what Rate of Compound Interest shall the Purchaser have for his money at that price?

$$500 ) 35.00 (.07 = R - 1.$$

Add 1.00

$$\hline 1.07 = R.$$

Fur

128 *Of Compound Interest.*

Furthermore, if it be inquired how many years Purchase any Annuity is worth, putting  $R$  = the Ratio as before, and  $Y$  the number of Years, the Rule is:

$$\frac{1}{R-1} = Y:$$

That is, Divide Unity by the Ratio less 1; and the Quote informs the Number of Years.

*Example.*

There is a Free-hold Estate to be sold, *Q.* How many Years Purchase is it worth at 5 per Cent. per Annum?

$$\begin{array}{r} .05 \ ) \ 1.0 \ (20 \\ \underline{\phantom{00000}} \\ 0 \end{array}$$

The Answer is 20 Years Purchase.

What is it worth at 6 per Cent. per Annum?

$$\begin{array}{r} .06 \ ) \ 1.0 \ (16.666 \\ \underline{40} \\ 40 \\ \underline{40} \\ 40 \\ \underline{40} \\ 4 \end{array}$$

The Answer is 16 Years, and  $\frac{2}{3}$  of a Year.

Again



Again, if an Estate be offered at any number of Years Purchase, and it be demanded what Rate of Interest the Purchaser shall have for his Money, the Rule is :

$$R = \frac{1}{Y} + 1.$$

That is, Divide Unity by the number of Years propos'd, and the Quote exhibits the Ratio, less Unity.

*Example.*

An Estate is offered at 20 Years Purchase, what Rate of Interest shall the Purchaser then have?

$$\begin{array}{r} 20 \overline{) 1.00} \quad (.05 \\ \text{Add } 1.00 \\ \hline 1.05 \end{array}$$

The Answer is 5 per Cent. per Annum.

There are many Tables of Compound Interest Printed in fundry Books for the valuation of Leases and Annuities, but they are generally made for yearly Payments, when indeed by the common and most usual Covenants in Leases the Tenant is obliged to pay quarterly; and in Leases of great value, there will be found a considerable difference in the true worth, (so great, that 25 l. per Quarter is as good as 102 l. 5 s. per Annum.) I have therefore presented the Reader with a Table fitted to such Quarterly Payments, the Use of which Table I doubt not but will be very easily found by the Examples that follow.

*A Table of Interest, for the Valuation  
of Leases or Annuities for Quarterly  
Payments, at 6 per Cent. per Annum,  
Compound Interest, for 31 Years.*

1	.985538	21	17.960417
2	1.956824	22	18.686219
3	2.914064	23	19.401524
4	3.857459	24	20.106484
5	4.787213	25	20.801250
6	5.836372	26	21.485968
7	6.609520	27	22.160789
8	7.496573	28	22.825841
9	8.373700	29	23.481282
10	9.238139	30	24.127242
11	10.090079	31	24.763844
12	10.929724	32	25.391256
13	11.757176	33	26.009595
14	12.572685	34	26.618988
15	13.376402	35	27.219206
16	14.168496	36	27.811474
17	14.949134	37	28.394861
18	15.718484	38	28.969764
19	16.476707	39	29.536352
20	17.223982	40	30.094714

41	30.645034	66	42.092531
42	31.187396	67	42.469245
43	31.721914	68	42.841611
44	32.248000	69	43.206601
45	32.767870	70	43.567307
46	33.279531	71	43.922768
47	33.783794	72	44.273138
48	34.280753	73	44.618415
49	34.843000	74	44.958701
50	35.253244	75	45.194062
51	35.728999	76	45.624577
52	36.197819	77	45.950311
53	36.659861	78	46.271331
54	37.115237	79	46.587715
55	37.564028	80	46.899521
56	38.006330	81	47.206817
57	38.442234	82	47.509668
58	38.871893	83	47.808141
59	39.295222	84	48.102298
60	39.712487	85	48.392200
61	40.123777	86	48.677877
62	40.529043	87	48.959492
63	40.928469	88	49.236993
64	41.322133	89	49.510486
65	41.710087	90	49.780023

91	50.045601	111	54.620966
92	50.307460	112	54.816601
93	50.665471	113	55.009461
94	50.819753	114	55.199474
95	51.070356	115	55.386751
96	51.317335	116	55.571297
97	51.560742	117	55.753185
98	51.841984	118	55.932443
99	52.037044	119	56.109107
100	52.271047	120	56.283219
101	52.499677	121	56.454811
102	52.725986	122	56.623921
103	52.949021	123	56.790588
104	53.134301	124	56.954843
105	53.385474	—	—
106	53.598963		
107	53.809375		
108	54.016743		
109	54.221113		
110	54.422527		

# Of Compound Interest. 133

The Calculation of a Number in the precedens Table, by aid of the Canon.

The Question being, What is the present worth of 1 l. per Quarter for 21 Years?

The Logarithm of the Increase of 1 l. at 6 per Cent. for three months = 0,0063264664  
The Number of Quarters = 84

$$\begin{array}{r} 253058656 \\ 506117312 \\ \hline \end{array}$$

Discompt of 1 l. for 84 Qrs. 0,5314231776

Then by the Rule of Proportion :

1,467384617 *com. arithm.* 9,8334569382  
have 100 l. for its Principal, 2,0000000000  
what shall 1 l. have for its Pr. 0,0000000000

$$68.148601 = 1,8334569382$$

The Log. of the Discompt = 0,5314231776

$$\begin{array}{r} 20.046279 \\ \hline 1,3020337606 \end{array}$$

$$48.102322$$

The Answer is = 48 l. 2 s. 0 d.  $\frac{1}{2}$  ferè.

And after this manner may a Table be Calculated, or the Value of a Lease for any Number of Years, may be found at any Rate of Interest required.

## The USE of the TABLE.

This Table sheweth the Discompt of 1 *l.* per Quarter at 6 per Cent. per Annum, Compound Interest, and if the Tabular Number for so many Quarters as the Lease is to continue be multiplied by the Quarterly Payment, that Product is the present Value of that Lease in ready money.

*Example.*

A Lease of 40 *l.* per Annum (*viz.* 10 *l.* per quarter) for 21 years, being to be sold, what is it worth in ready money?

84 quarters per Table = 48.102221

The quarterly Rent = 10

481.022210

The Answer is 481 *l.* 0 *s.* 5 *d.*  $\frac{3}{4}$  ferè.

But if the question be, What quarterly Rent for 21 years will a given Sum purchase? Then divide the given Sum by the Tabular Number for so many quarters.

*Example.*

48.102221 ) 481.022210 ( 10

000000

A Gentleman having a Lease of certain Church Lands, worth 200 *l.* per Annum more than the reserved Rent, for 14 years to come, surrenders the same, upon condition the Chapter shall make him a new Lease for 31 years without a present Fine, but advancing the old Rent 10 *l.* per quarter during the whole term of 31 years; what doth he gain by the bargain, accompting Compound Interest on both sides?

$$\begin{array}{r} 56 \text{ quarters per Table} = 38.006 \\ \text{The quarterly Rent} = \quad 50 \\ \hline 1900.300 \end{array}$$

$$\begin{array}{r} 124 \text{ quarters per Table} = 56.955 \\ \quad 40 \\ \hline 2378.200 \\ 1900.300 \\ \hline 377.9 \end{array}$$

The Answer is 377 *l.* 18 *s.* the new Lease being so much more worth than the old one.

240 *l.* is demanded for the Lease of a House for 7 years, the Tenant offers 100 *l.* and an advance of Rent equivalent to the rest of the Fine required, what ought this Rent to be?



# 136 Of Compound Interest.

$$\begin{array}{r}
 28 \text{ quarters} = 22.8258) 140.0000 (6.1334 \\
 \underline{304520} \\
 762620 \\
 \underline{778460} \\
 936760
 \end{array}$$

The Advance of Rent ought to be 6 l. 2 s. 8 d. per quarter.

There is a Lease of 200 l. per Annum, viz. 50 l. per quarter, for  $13 \frac{1}{4}$  years, to be sold, what is it worth at 6 per Cent. Simple, and what at 6 per Cent. Compound Interest?

*Simple.*

$$\begin{array}{r}
 53 \text{ quarters per Table} = 38.779748 \\
 \underline{50} \\
 1938.987440
 \end{array}$$

*Compound.*

$$\begin{array}{r}
 53 \text{ quarters per Table} = 36.659861 \\
 \underline{50} \\
 1832.993050
 \end{array}$$

Which subtracted from 1938.987440

Leaves 105.99439

Whereby it appears, that it is cheaper to the Purchaser at Compound Interest than at Simple Interest by 106 l.

*Six Questions performed by the aid of the Canon of Logarithms.*

*Quest. 1.* A Gentleman pays 350 *l.* for a Lease in Reversion, to commence at the end of 13 years and a quarter, and to continue for 21 years and 3 quarters, what quarterly Rent may he lett the Premises for, after he comes to be in possession thereof, so as to gain 8 *per Cent.* Compound Interest for his money?

The Logarithm of 350 *l.* = 2,544008  
Worth of 1 *l.* forborn 53 quarters = 0,442865

Log. of the Increase of 350 *l.* = 2,986873  
Worth of 1 *l.* for 87 quarters = 1,621420

Log. of 23.198 = 1,365453

The Answer = 23 *l.* 3 *s.* 11 *d.*  $\frac{1}{2}$  *ferè.*

*Quest. 2.* A Citizen having taken a Lease of a House and Shop for 21 years, at 370 *l.* Fine, and 100 *l.* *per Annum*, viz. 25 *l.* *per* quarter, Rent, at the end of two years is willing to leave it for 300 *l.* and the old Rent, or to have such an increase of Rent, during the whole term yet to come, as may reimburse him his Fine paid, with Compound Interest at 6 *per Cent.* *per Annum*: What ought

# 138      *Of Compound Interest.*

ought he to receive in advance of Rent, and what doth he offer to lose of his Fine paid in taking 300*l*.

$$2,568202 = 370 \text{ } l.$$

1,682165 = The worth of 1 *l*. per quarter  
for 84 quarters.

0,886037 The Advance of Rent ought to  
be 7 *l*. 13 *s*. 10 *d*.  $\frac{1}{4}$  *ferè*.

1,652198 The worth of 1 *l*. per quarter  
for 76 quarters.

2,545235 The present Fine ought to be  
350 *l*. 18 *s*. 10 *d*.

Whereby it appears, there is 50 *l*. 18 *s*.  
10 *d*. offered to be lost in putting off the House  
and Shop aforementioned.

*Quest. 3.* *A* sells a House to *B* for 800 *l*. to be  
paid with Interest upon Interest by 100 *l*.  
per Annum, viz. 25 *l*. per quarter, how  
many quarters Rent ought *B* to pay before  
*A* is satisfied for his 800 *l*. with Compound  
Interest at 6 per Cent. per Annum, and what  
ought the last Payment be?

*As*

# Of Compound Interest.

139

As 1.46738

to 100

So 25

to 1703.71

800

903.71

Its Logarithm = 2,956028

0,275369

Log. of 1 l. forborn 1 quarter 0,006326

006326 ) 275369 ( 43 quarters,

23329

3351

The Rent 25 1,397940

1 l. per quarter for 43 quarters 1,501359

793.047 = 2,899299

800

6.953 its Logar. 0,841049

Log. of amount of 1 l. for 44 quarters 0,278364

1,119413

The last Payment 13 l. 3 s. 4 d. ferè.

Quest.

*Quest. 4.* *A* lends unto *B* a certain Sum of ready money, and accepts a Rent Charge of 40*l.* quarterly for 7 years in satisfaction; finding it paid him his Principal with Interest upon Interest at 8 *per Cent.* within 13 *l.* 4*s.* 6*d.* what was the Money lent?

1,601060 The Logarithm of 40 *l.*

1,565196 The Logarithm of the worth of 1 *l.*  
 quarterly for 48 quarters.

3,167256 The Logarithm of the worth of 40*l.*  
*per quarter* for 48 quarters.

$$\begin{array}{r} 3,167256 = 1469.787 \\ \quad \quad \quad 13.225 \\ \hline \end{array}$$

3,163328 = 1456.562

0,177140 The Logarithm of the increase of  
 1 *l.* forborn 28 quarters.

2,986188 The Logarithm of 968.7.

The Money lent was 968 *l.* 14*s.*

*Quest. 5.* A Testator leaving one Son and two Daughters, bequeaths out of his Estate (being 600 *l.* *per Annum* for 11 years) to his eldest Daughter 500 *l.* *per Annum* for 4 years next coming, at the end whereof, to his younger Daughter 300 *l.* *per Annum* for 7 years, and to his Son the Remainder of the Estate

# Of Compound Interest.

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Estate for the whole time: 2. Which had the greatest Portion, and by how much, calculating their several Annuities at 6 per Cent. Compound Interest?

0,539716 Logarithm of the worth of 1 l. per annum for 4 years.

2,698970 The Logarithm of 500 l.

---


$$3,238686 = 1732.55.$$

0,746820 The Logarithm of the worth of 1 l. per annum for 7 years.

2,477121 The Logarithm of 300 l.

---

3,223941

0,101232 The Logarithm of the worth of 1 l. forborn 4 years.

---


$$3,122709 = 1326.47.$$

0,896905 The Log. of the present worth of 1 l. per annum for 11 years.

---

2,000000

---


$$2,896905 = 788.68$$

0,746820

142 *Of Compound Interest.*

0,746820 The Log. of the present worth of  
1 *l.* per annum for 7 years.

2,301029 The Logarithm of 200 *l.*

---

3,047849

0,101232 The Logarithm of the worth of 1 *l.*  
forborn 4 years.

---

2,946617 = 884.34

788.68

---

1673.02

The Sons Portion ————— 1673 : 00 : 05

The eldest Daughters Portion 1732 : 11 : 00

The youngest Daughters — 1326 : 09 : 04 $\frac{1}{4}$

---

4731 : 19 : 09 $\frac{1}{4}$

*Proof.*

0,896905 The Logarithm of the worth of  
1 *l.* per annum for 11 years.

2,778151 The Logarithm of 600 *l.*

---

3,675056 The Logarithm of 4732 *l.*

*Quest. 6.* A Merchant sold 16 Kintals of Cyprus Cottons for 320 *l.* to be paid at two six-months; the Buyer having Money by him, offers to pay the Money presently,  
pro-



*Of Compound Interest.* 143

provided the Merchant allow him Discompt  
at 6 per cent. Compound Interest. Q. What  
ought the Merchant to receive?

- 2,505149 The Logarithm of 320 l.  
0,018979 The Logarithm of 1 l. forborn 9  
months, the equated time, acor-  
ding to the Table of Mean  
Time, *Pag.* 110.  
2,486170 The Logarithm of 306.316.

The Answer 306 l. 6 s. 4 d. ferè.

---

STE-

---

provided the Member shows him 13 coupons  
and a certain amount of interest. What  
ought the Member to receive?

The Answer Book is a book  
The Answer Book is a book  
The Answer Book is a book

# STEREOMETRY:

OR,

A New and the most Practical Way

OF

## Gauging Tunns

*In the form of a*

PRISMOID & CYLINDROID:

ALSO

*The Frustums of Pyramids and of a Cone.*

Together with

The *Art* of CASK-GAUGING.

---

By *John Mayne.*

---

London, Printed by *William Godbid*, for  
*Nath. Crowch*, in *Exchange-Alley*.

M. DC. LXXIII.

STEEPLEHOMES

A New and Improved Fashioned Way

Gauging Tunnels

THEORY AND PRACTICE

OF THE ART OF GAUGING

THEORY AND PRACTICE

By John Mayne

Printed by William Goddard, for  
Wm. Goddard, in Exchange Alley,  
Opposite the Old Exchange



TO THE  
Young Geometrician.

I Hope by this time thou art so sufficiently acquainted with the Nature and Use of a Decimal Fraction, that any Operation in the six Species, viz. Addition, Subtraction, Multiplication, Division, Involution and Evolution of the Second and Third Powers, will not appear difficult to thee; and these being familiar, any Calculation in Arithmetick, Geometry, Trigonometry, or other Mathematical Arts, will not seem strange: Amongst the many pleasant walks in this Tempe, I have made it my present design to give thee some diversion in that part of Solid Geometry called Gauging, and herein passing by those Blossoms that kiss the hand of every Passenger, I have endeavoured (and I hope not altogether without success) to shew thee how to gather a Rose without danger of its Thorn: For the In-

L 2

vention,

[ ]

vention, the world is obliged to the Ingenious Mr. Michael Dary, the Roots of these, and many other choice Mathematical Flowers, lying crowded together in a small Treatise called Dary's Miscellanies, Printed 1669. Here, as in the former Part, thou hast both Precept and Example in the plainest method I could possibly expresse them. That they may by no means seem obscure to any ingenious Student, is the hearty desire of

Thy Friend,

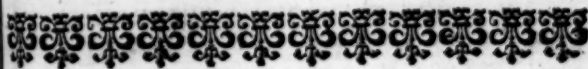
J. M.

The



# The Explanation of the Signs or Characters.

+	More.
-	Less.
=	Equal.
>	Greater.
<	Lesser.
x	Multiplied.
√	Square Root.
q	Square.
⊙	Circle.
::	Proportional.
∞	Difference.





# The Examination of the Signs of Character

1. The face	✓
2. The eyes	✓
3. The nose	✓
4. The mouth	✓
5. The ears	✓
6. The hair	✓
7. The hands	✓
8. The feet	✓
9. The voice	✓
10. The gait	✓
11. The dress	✓
12. The manners	✓
13. The conversation	✓
14. The writing	✓
15. The signature	✓



# STEREOMETRY:

OR,

A New and the most Practical Way of  
GAUGING TUNNS, &c.

---

*A plain and easie Method for finding the  
Solid Content of a Prismoid.*

## DEFINITION.

**B**Y the word *Prismoid* is to be understood  
a Solid contained under six plain Sur-  
faces, whereof the two Bases ought to  
have these three qualifications:

1. Rectangular Parallelograms.

2. Parallel.

3. Alike Situate. *i. e.* So situate, that the  
Rectangular Conjugates in both Bases may be  
inserted by two and the same Planes, and a  
Right Line extended from the Center of one  
Base to the other may be called the Axis, and  
the other remaining four Planes are the Peri-

*patafma*. Under this Definition is comprehended the Frustrums of Pyramids and Prisms.

*Note also*, If the *Peripatafma* be not made by the four flat Sides (spoken of before) but shall be constituted by Curvature from Circles or Elipse's, the Solid is then called a *Cylindroid*, and under this Definition is comprehended Frustrums of Cones and Cylinders.

### PROBL.

If in a *Prismoid* you put

$C$  = the whole Content thereof.

$A$  &  $B$  = the two Rectangular Conjugates above.

$G$  &  $H$  = the two Rectangular Conjugates below.

$A$  &  $G$  opposite = their two Correspondents one above the other below inserted by one Plane.

$B$  &  $H$  opposite = their two Correspondents above and below; and also inserted by one Plane.

$P$  = the perpendicular height of the Prism or Prismoid.

$K$  = the increment of any two Diameters, to be taken between  $A$  and  $G$  in the same Plane with them, at one Inch distance of the perpendicular.

$L$  = the increment of any two Diameters, to be taken between  $B$  and  $H$  in the same Plane with them, at one Inch distance of the perpendicular.

Then,

Then,

Analogism.

$$) G H P + \frac{1}{2} \left\{ \begin{matrix} G L \\ H K \end{matrix} \right\} P P + \frac{1}{3} K L P P P (= C.$$

Or,

The Rectangle of the two Diameters at the Base multiplied into the Perpendicular, more the Semi-sum of G L and H K, (*viz.* those two Diameters multiplied into their altern increments) multiplied into the Square of the Perpendicular, to which add one third of the Rectangle of K L (*i. e.*) the two increments multiplied into the Cube of the Perpendicular is equal to the Content in Cubick Inches.

By which *Theorem* you find three fixed or stationary Numbers, which Mr. Dary calls *reserved Coefficients*, wherefore you shall find them hereafter called by that denomination: These three reserved Coefficients thus multiplied into the Perpendicular, the Product is equal to the whole Content, or by any part of the Perpendicular gives the Solidity of that part.

Prop. I.

Having a Tunn in the form of a Prismoid, the Dimensions being, *Disproportional*

$$\left. \begin{array}{l} A = 126 \text{ and } B = 144 \\ C = 102 \text{ and } H = 108 \\ P = 60 \end{array} \right\} \begin{array}{l} \text{above.} \quad \text{above.} \\ \text{below.} \quad \text{below.} \end{array} \text{Inches.}$$

What

*What is the Solidity of this Tunn in Cubick Inches?*

First then to find the three reserved Coefficients.

$$\begin{array}{c} A - G \\ P = 60 ) 24.0 (.4 = K. \end{array}$$

i. e. The difference between A and G (the two opposite Diameters above and below) divided by the Perpendicular quotes K, the increment of any two Diameters to be taken between them, at one Inch distance in the Perpendicular, and in the same Plane.

$$\begin{array}{c} B - H \\ P = 60 ) 36.0 (.6 = L. \end{array}$$

That is, the difference between B and H (the two Diameters opposite the one above the other below) divided by the Perpendicular quotes L, the increment of any two Diameters to be taken between them, at one Inch distance in the Perpendicular, and in the same Plane with them.

$$.6 = L$$

$$.4 = K$$

$$a = .24 = \text{The Rectangle of } L \text{ } K$$

$$.08 = \frac{1}{3} \text{ of } L \text{ } K, \text{ the first Coefficient.}$$

# Practical Gauging.

155

$$102 = G$$

$$108 = H$$

$$.6 = L$$

$$.4 = K$$

$$\begin{array}{r} 61.2 = GL \\ 43.2 \end{array}$$

$$\begin{array}{r} 43.2 = HK \end{array}$$

$$104.4 = GL + HK$$

$$b = 52.2 = \frac{1}{2} GL + HK, \text{ the second Coefficient}$$

$$102 = G$$

$$108 = H$$

$$816$$

$$1020$$

$$\left. \begin{array}{l} GH + \frac{1}{2} GL + HK \\ + \frac{1}{2} LK = \text{first junk} \\ GH + \frac{1}{2} GL + HK + \\ LK = 2.333 = 2^{\text{d}} \text{ diff} \end{array} \right\}$$

$$c = 11016 = GH, \text{ the third Coefficient.}$$

Now having found these reserved Coefficients, I proceed, and finding that  $\frac{1}{3}$  of KL must be multiplied by the Cube of the Perpendicular, I begin with it, and call that the first Coefficient; then  $\frac{1}{2} \left\{ \begin{array}{l} GL \\ HK \end{array} \right\}$  being to be multiplied by the Square of the Perpendicular, I add that to the first Fact, and call it the second Coefficient; lastly, GH being to be multiplied by the Perpendicular, I add that to the second Fact, and call it the third Coefficient; then will the Work stand thus:

$$\begin{array}{l} c + b + \frac{1}{3} a = \text{first junk} \\ c + 3b + a \times 2.333 = 2^{\text{d}} \text{ junk} \text{ Example} \\ 2b + 4a = 2^{\text{d}} \text{ Diff.} \\ 2a = 3^{\text{d}} \text{ Diff.} \end{array} \left\{ \begin{array}{l} 11068.28: 1 \text{ junk} \\ 11173.16: 2 \text{ junk} \\ 105.36: 2 \text{ Diff.} \\ .48.3 \text{ Diff} \end{array} \right.$$

## Example.

 $.08 =$  first Coefficient. $60 =$  the Perpendicular.

---

 $4.80$  $52.2 =$  second Coefficient.

---

 $57.0$  $60 =$  the Perpendicular.

---

 $3420$  $11016 =$  third Coefficient.

---

 $14436$  $60 =$  the Perpendicular.

---

**The Answer 866160 Cubick Inches.**

Now admitting this Tunn have but 33 wet  
Inches, what is the Content thereof?

 $.08$  $33$  $24$  $24$ 

---

 $2.64$  $52.2$ 

---

 $54.84$



$$\begin{array}{r}
 54.84 \\
 33 \\
 \hline
 16452 \\
 16452 \\
 \hline
 1809.72 \\
 11016 \\
 \hline
 12825.72 \\
 33 \\
 \hline
 3847716 \\
 3847716 \\
 \hline
 \end{array}$$

The Answer = 423248.76 Cubick Inches.

Prop. II.

Having a Tunn in the form of a Prismoid, the Dimensions being,

$$\begin{array}{lcl}
 \text{above.} & & \text{above.} \\
 G = 102 \text{ and } H = 108 & & \\
 \text{below.} & & \text{below.} \\
 A = 126 \text{ and } B = 144 & & \\
 P = 60 & & 
 \end{array}
 \left. \vphantom{\begin{array}{lcl} \text{above.} \\ G = 102 \text{ and } H = 108 \\ \text{below.} \\ A = 126 \text{ and } B = 144 \\ P = 60 \end{array}} \right\} \text{Inches.}$$

What is the Solidity in Cubick Inches?

To find this Tunns Solidity, the Rule is:

$$ABP - \frac{1}{2} \left\{ \frac{AL}{BK} \right\} PP + \frac{1}{3} KLP PP = \text{Content.}$$

i. e. The Fact of A B (the rectangular Conjugates

gates at the Base) multiplied by the Perpendicular, from whence subduct the Semi-sum of the two Facts (A and its altern decrement, B and its altern decrement, multiplied into the Square of the Perpendicular) more the one third of the Rectangle of KL, viz. the two decrements, multiplied into the Cube of the Perpendicular; and that Remainder is the Content in Cubick Inches.

To find the Coefficients

$$\begin{array}{r} G - A \\ P = 60 ) - 24.0 ( - .4 = K. \end{array}$$

$$\begin{array}{r} H - B \\ P = 60 ) - 36.0 ( - .6 = L. \end{array}$$

This Rule being the Converse of the former, these Numbers K and L which before were Affirmatives are now become Negatives (then increment, now decrement,) the greater Conjugates being subducted from the lesser makes the Dividends so much less than nothing; and consequently the Quotes, the Divisor being an Affirmative, yet these two Negatives being multiplied together, their Fact becomes Affirmative, according to the Rule of *Algebra*, the Signs of the Factors being homogeneal (or alike) makes the Fact more, as in this

*Example.*

Example.

$$\begin{array}{r} - .6 = L \end{array}$$

$$\begin{array}{r} - .4 = K \end{array}$$

$$\begin{array}{r} + .24 \end{array}$$

$$\begin{array}{r} + .08 = \frac{1}{3} LK \text{ the first Coefficient.} \end{array}$$

$$\begin{array}{r} 126 = A \end{array}$$

$$\begin{array}{r} - .6 = L \end{array}$$

$$\begin{array}{r} - 75.6 \end{array}$$

$$\begin{array}{r} - 57.6 \end{array}$$

$$\begin{array}{r} - 133.2 \end{array}$$

$$\begin{array}{r} 144 = B \end{array}$$

$$\begin{array}{r} - .4 = K \end{array}$$

$$\begin{array}{r} 57.6 \end{array}$$

$$-66.6 = \frac{1}{2} AL + BK, \text{ second Coefficient.}$$

The Factors in these Rectangles being heterogeneous (or unlike) the Fact is made less.

$$\begin{array}{r} 126 = A \end{array}$$

$$\begin{array}{r} 144 = B \end{array}$$

$$\begin{array}{r} 504 \end{array}$$

$$\begin{array}{r} 504 \end{array}$$

$$\begin{array}{r} 126 \end{array}$$

$$18144 \text{ The third Coefficient.}$$

These two Factors being both Affirmatives, the Fact is +.

With

With these three reserved Coefficients I proceed to the Calculation, according to the precedent Theorem.

$$+.08 = \text{the first Coefficient.}$$

$$60 = \text{the Perpendicular.}$$

$$+4.80$$

$$-66.6 = \text{second Coefficient.}$$

$$-61.8$$

$$60 = \text{the Perpendicular.}$$

$$-3708.0$$

$$+18144 = \text{third Coefficient.}$$

$$14436$$

$$60 = \text{the Perpendicular.}$$

The Answer = 866160 Cubick Inches.

But if this Tunn have only 27 Inches of the Perpendicular wet, the Content then being required:

$$+.08$$

$$27$$

$$56$$

$$16$$

$$2.16$$

$$-66.6$$

$$-64.44$$

$$= 64$$

# Practical Gauging.

101

—64.44

27

45108

12888

—1739.88

+18144

+16404.12

27

11481884

3280824

The Answer = 442911.24 Cubick Inches.  
423248.76

Proof. 866160

Prop. III.

There is a *Tun* in the form of a *Prismoid*, the Dimensions are,

above.

above.

A = 132 and B = 144

below.

below.

G = 108 and H = 108

P = 60

Inches.

What is the Solidity in Cubick Inches?

M

P = 60

A—G

$$P = 60 ) 24.0 (.4 = K.$$

B—H

$$P = 60 ) 36.0 (.6 = L.$$

.6

.4

.24

.08 = the first Coefficient.

$$G = 108$$

$$L = .6$$

$$64.8$$

$$43.2$$

$$108.0$$

$$H = 108$$

$$K = .4$$

$$43.2$$

54 = the second Coefficient.

$$108$$

$$108$$

$$864$$

$$1080$$

11664 = the third Coefficient.

$$\begin{array}{r}
 .08 \\
 60 \\
 \hline
 4.80 \\
 54 \\
 \hline
 58.8 \\
 60 \\
 \hline
 3528.0 \\
 11664 \\
 \hline
 15192 \\
 60 \\
 \hline
 \end{array}$$

The Answer = 911520 Cubick Inches.

Prop. IV.

There is a Tunn in the form of a Prismoid, the Dimensions being above.

$$\begin{array}{l}
 G = 108 \text{ and } H = 108 \\
 \text{below.} \qquad \qquad \text{below.} \\
 A = 132 \text{ and } B = 144 \\
 P = 60
 \end{array}
 \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \text{Inches.}$$

What is its Solidity in Cubick Inches?

The reserved Coefficients are found to be :

$$\begin{array}{l}
 G = A \\
 P = 60 \text{ ) } - 24.0 \text{ ( } - .4 = K.
 \end{array}$$

M 2

P = 60



$$P = 60) \overset{H-B}{-36.0} (-.6 = L.$$

$$-.6$$

$$-.4$$

$$-$$

$$+.24$$

$$-$$

$$+.08 = \text{the first Coefficient.}$$

$$A = 132$$

$$L = -.6$$

$$-79.2$$

$$-57.6$$

$$-136.8$$

$$-68.4 = \text{the second Coefficient.}$$

$$132$$

$$144$$

$$528$$

$$528$$

$$+.19008 = \text{the third Coefficient.}$$

The

The Calculation.

$$\begin{array}{r}
 + .08 \\
 \hline
 60 \\
 + 4.80 \\
 \hline
 - 68.4 \\
 \hline
 - 63.6 \\
 \hline
 60 \\
 \hline
 - 3816.0 \\
 \hline
 + 19008 \\
 \hline
 + 15192 : \\
 \hline
 60
 \end{array}$$

The Answer = 911520 Cubick Inches.

Here note, if any of the precedent Tunns be cloathed by Curveture; (*i. e.* the Bases being Circular or Elliptical) the last Product ought to be divided by 1.27324, then will the Quotient exhibit the Cubick Inches in that Solid. But if the Question be Ale Gallons, let your Coefficients be divided by 282; if Beer Barrels be required, divide the Coefficients by 10152, the number of Inches in a Beer Barrel. In all flat sided Figures, and for those Solids, whose Peripatasma is constituted by Circles or Ellipsis, the Divisor for Beer Barrels is 12926 >, for Ale Barrels 11490 >,

M 3

and

and for Ale Gallons 359; of which take these Examples.

*What number of Beer Barrels and Gallons doth the last mentioned Tunn contain?*

The three Coefficients for Beer Barrels divided by 10152 are:

$$\text{The first} = +.000007880220646 <$$

$$\text{The second} = -.0067375888 >$$

$$\text{The third} = + 1.8723404 <$$

The three Coefficients for Gallons being divided by 282 are:

$$\text{The first} = .0002837 >$$

$$\text{The second} = .2425532 >$$

$$\text{The third} = 67.4042553 >$$

The Coefficients being thus fitted, the Calculation is after this manner:

*For Barrels.*

$$+.00000788 <$$

60

---


$$+.00047280$$

$$-.00673758$$

---


$$-.00626478$$

$$-.00626478$$

# *Practical Gauging.*

867

$$-.00626478$$

60

$$-.37588680$$

$$+1.8723404$$

$$1.4964536$$

60

$$89.7872160$$

The Answer is 89 Barrels, 3 Firkins, and 1  
Gallon, or 89 Barrels and 28 Gallons.

*For Gallons.*

$$+.0002837 >$$

60

$$+.0170220$$

$$-.2425532$$

$$-.2255312$$

60

$$-13.531872$$

$$+67.404255$$

$$53.872383$$

60

$$3232.342980$$

M 4

The

The Answer is 3232 Gallons, which divided by 36 quotes 89 Barrels 28 Gallons, as before.

*Example.*

36 ) 3232 ( 89 Bar.

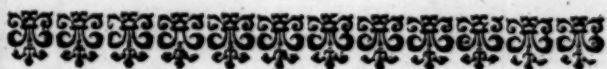
352

28 Gall.

A



A New Way of  
**GAUGING**  
THE  
*Frustum* of a **PYRAMID**  
OR  
**CONICAL TUNN.**



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A New Way of

GALLING

THE

Principle of a PLANNED

OR

CONICAL TOWN

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A New Way of  
GAUGING

THE

*Frustrum of a Pyramid, &c.*

DEFINITION.

**A** *Pyramid* is a Solid Figure, contained under many Superficies, whereof one is the Base, and the rest arise from the Base to the Vertex, and there meet in a Point.

The *Frustrum* of a *Pyramid* is a Solid, cut with a Plane parallel to the Base, and the part cut off is also a *Pyramid*.

The *Frustrum* of a *Cone*, may not improperly be termed the *Frustrum* of a round *Pyramid*, (the Base being circular) nor do I think it an Heresie to call a *Cylinder* a round *Prism*.

The *Frustrum* of a *Pyramid*, whose Bases are in the form of any ordinate Polygon, being alike, and alike situate, and also if a Right  
Line

Line may be every where applied in the *Peripatasma* from Base to Base, moreover a Right Line being extended from the Center of one Base to the other, may be called the Axis.

Then if you put

$S$  = the whole Solidity.

$B$  = a Side above.

$A$  = a Side below.

$P$  = the Perpendicular.

$d$  = the common Addend at one Inch distance of

the Perpendicular, and is thus made  $\frac{B-A}{P} d$ ,

that is, the difference between a Side above and a Side below, divided by the Perpendicular, quotes the increment, &c.

$G$  = the Divisor.

The Rule is:

$$G) A A p + A d p p + \frac{1}{3} d d p p p (= S$$

Or, in other terms:

To the Square of the Side multiplied by the Perpendicular, add the Fact of one Side in the Increment multiplied by the Square of the Perpendicular, more  $\frac{1}{3}$  of the q. of the Increment in the Cube of the Perpendicular, and the Aggregate divided by the Polygons respective Divisor, the Quote will be the Solidity.

And further it is to be well observed, if your Frustum of a *Pyramid* stand upon its greater Base, the Rule then is thus varied:

$$G): B B p - B d p p + \frac{1}{3} d d p p p (= S$$

That

That is to say :

From the Square of a Side at the Base multiplied by the Perpendicular, subtract the Rect. angle of one of those Sides in the Decrement multiplied by the Square of the Perpendicular, more one third of the Square of the Decrement in the Cube of the Perpendicular, and that Remainder divided by the Divisor proper to the form of the Base, the Quote is equal to the Solidity.

Note also, that *p* may be put for a part of the Perpendicular, and the Answer will be the Content of that part required.

G) or the Divisors for these 8 Regular Polygons, and the Cone.

For Cubick Inches.		For Ale Gallons.	
Trigon	2.30940	Trigon	651.2000
Tetragon		Tetragon	282.0000
Pentagon	.58123	Pentagon	157.2600
Hexagon	.38497	Hexagon	108.5400
Heptagon	.27513	Heptagon	77.5867
Octogon	.20710	Octogon	58.4022
Nonogon	.16176	Nonogon	45.6163
Decagon	.12997	Decagon	36.6515
Cone	1.27324	Cone	359.0500

If your Tunn be the Fruustum of a Cone :

Let  $A$  or  $B$  be the Diameter at the Base, and  $d$  the Increment or Decrement of any two Diameters between  $A$  and  $B$ , at one Inch distance of the Perpendicular, and the Divisor as per Table.

I shall only give you some Examples of the three first, and the Cones Fruustum, which I think will be sufficient to inform any ingenious Practitioner how to perform the rest.

### The Trigon.

Admit a Tunn be in the form of an equilateral Triangle, the Dimensions being,  
 $A = 126$  Inches, the length of a Side above,  
 $B = 108$  Inches, the length of a Side below,  
 $P = 60$  Inches, the Perpendicular,  
 Q. The Content in Ale Gallons?

The Coefficients are found, according to the precedent directions, thus :

$$A \rightarrow B$$

$$P = 60 \quad 240 \quad .4 = d \text{ the Increment}$$

$$.4$$

$$.16 = dd$$

$$.05333 \text{ first Coefficient.}$$

$$102 = B$$

$$.4 = d$$

40.8 the second Coefficient.

$$102$$

$$102$$

$$\hline$$

$$204$$

$$1020$$

$$\hline$$

10404 the third Coefficient.

These three divided by the Divisor for Ale Gallons, viz, 65 L. 2, are as followeth:

$$\text{The first Coefficient} = .000082$$

$$\text{The Perpendicular} = 60$$

$$.004920$$

$$\text{The second Coefficient} = .06265$$

$$.06757$$

$$60$$

$$4.05420$$

$$\text{The third Coefficient} = 15.9775$$

$$20.0317$$

$$60$$

$$\text{The Answer} = 1201.9020 \text{ Ale}$$

Gallons.

A Tunn

A Tunn of the same Dimensions standing upon its greater Base, the Coefficients are thus found :

$$\begin{array}{r}
 B - A \\
 P = 60 ) 24.0 ( - .4 \\
 \underline{-.4} \\
 + .16
 \end{array}$$

.053333 first Coefficient.

126

— 50.4 the second Coefficient.

126  
126

756

252

126

15876 the third Coefficient.

Being divided by the same Divisor with The former, they are :

+ .000082

— .077395

+ 24.380000

And

# *Practical Gauging.*

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And are thus used :

$$\begin{array}{r} +.000082 \\ \hline 60 \end{array}$$

$$\begin{array}{r} +.004910 \\ \hline -.07739 \end{array}$$

$$\begin{array}{r} -.07247 \\ \hline 60 \end{array}$$

$$\begin{array}{r} -.434820 \\ \hline +24.38 \end{array}$$

$$\begin{array}{r} 20.0318 \\ \hline 60 \end{array}$$

The Answer as before = 1201.9080 Ale Gallons.

Now if each of these Tunns have 30 Inches of the Perpendicular wet, how much do they contain ?

The First.

$$\begin{array}{r} +.000082 \\ \hline 30 \end{array}$$

$$\begin{array}{r} +.002460 \\ \hline +.062565 \end{array}$$

$$\begin{array}{r} .065025 \end{array}$$

N

065025



$$+.065025$$


---


$$30$$

$$+.1950750$$


---


$$+.15.9775$$


---

$$+.17.92825$$


---


$$30$$

The Answer = 537.84750 Ale Gallons.

The Second.

$$+.00082$$


---


$$30$$

$$+.002460$$


---

$$-.07739$$


---

$$-.07493$$


---


$$30$$

$$-2.24790$$


---

$$+.24.38$$


---

$$+.22.1321$$


---


$$30$$

The Answer = 663.9630 Ale Gallons.

Proof.

$$663.9630$$

$$537.8475$$


---

$$1201.8105$$

The difference being less than a Pint.

The

# The Tetragon or Square Pyramid.

There is a Tunn in the form of the Frustum of a Square Pyramid,

A = 144 Inches, the length of a Side above,

B = 108 Inches, the length of a Side below,

P = 60 Inches, the Perpendicular,

Q. The Content in Gallons?

The Coefficients being found by the former Rule and Example, viz.

$$P) A - B (= d.$$

$\frac{1}{3}$  of  $dd$  = the first Coefficient .12 =

$dB$  = the second Coefficient 64.8 =

$BB$  = the third Coefficient 11664 =

These three being divided by 282 the Cubick Inches in the Ale Gallon, are equal to

The first Coefficient = .00042553  
60

The second Coefficient = .2298  
60

.02553180  
60  
15.3199080

$a+b+a$   
Content  
first York  
~~2nd York~~  
~~2nd York~~  
~~2nd York~~  
 $b+a$

The

	N 2	15	
$BB + dB \frac{1}{3} dd$	= Cont.	first York	viz 11728.92
$BB + 3dB + dd \times 2.333$	= 2 <sup>d</sup> York		11859.24
$2dB + 4dd$	= 2 <sup>d</sup> Difference		131.04
$2bb$	= 3 <sup>d</sup> Difference		.72

$$\begin{array}{r} 15.3199080 \\ \text{The third Coefficient} = 41.3617 \\ \hline 56.6816 \\ 60 \end{array}$$

$$\text{The Answer} = 3400.8960 \text{ Ale Gallons.}$$

If the Tunn stand upon its greater Base, the Coefficients then are  $P \vee B - A (= -d$ , and the  $\frac{1}{3} d d =$  the first,  $A d =$  the second, and  $A A =$  the third, which divided by 282 the number of Cubick Inches in an Ale Gallon, they do appear to be  $= +.00042553$  And if the Content be required 60

$$\begin{array}{r} .02553180 \\ - .306383 \\ \hline - .2808512 \\ 60 \\ \hline - 16.8510720 \\ + 73.532 \\ \hline + 56.680928 \\ 60 \end{array}$$

$$\text{The Answer} = 3400.855680$$

# *Practical Gauging.*

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If 40 Inches of the Perpendicular be wet in the first Tunn, and 20 in the latter, and it be demanded what they contain in Ale Gallons.

The first.

The second.

.00042553

+ .00042553

40

20

.01702120

+ .00851060

+ .2298

+ .306383

+ .2468212

+ .2978724

40

20

+ 9.8728480

+ 5.9574480

+ 41.3617

+ 73.532

51.234548

+ 67.574552

40

20

2049.381920

1351.491040

*Proof.*

210

2049.38

1351.49

3400.87

N 3

The

## The Pentagonal Pyramid.

A Tunn in the form of the Frustum of a Pyramid,  
whose Bases are in the form of a Pentagon,

A = 144 Inches, the length of each Side above,

B = 108 Inches, the length of each Side below,

P = 60 Inches, the Perpendicular,

Q. The Content in Ale Gallons?

The three Coefficients found in the last Example, viz,

$$P) A - B(d$$

For Ale Gall.

$$\frac{1}{3} dd = .12 \quad | = .0007632$$

$$Bd = 64.8 \quad | = .412126$$

$$BB = 11664 \quad | = 74.18274$$

$$.0007632$$

$$60$$

$$.0457920$$

$$.412126$$

$$.457918$$

$$60$$

$$27.475080$$

$$74.18274$$

$$101.65782$$

$$60$$

The Answer = 6099.46920 Ale Gall.

Let

Let another Fruustum of a Pyramid of the same Bases and Altitude, stand upon its greater Base, and the Content in Ale Gallons be demanded.

The Coefficients so found and divided as before directed, are as followeth:

The first Coefficient =  $\frac{+ .0007632}{60}$

$\frac{+ .0457920}{60}$

The second =  $\frac{- .5495}{60}$

$\frac{- .503708}{60}$

The third =  $\frac{+ 30.222480}{101.65752}$

The Answer = 6099.45120

If 50 Inches of the Perpendicular in the first Tunn be wet, and 10 Inches in the last, what is the Content in Ale Gallons?

N 4

The

The first.

The last.

.0007632	+ .0007632
50	10
<hr/>	<hr/>
.0381600	+ .0076320
412126	— .5495
<hr/>	<hr/>
450286	— .541868
50	10
<hr/>	<hr/>
22.514300	— 5.418680
74.18274	+ 131.88
<hr/>	<hr/>
96.69704	+ 126.46132
50	10
<hr/>	<hr/>
4834.85200	1264.61320

Proof.

4834.8520
1264.6132
<hr/>
6099.4652

A Tunn in the form of a Frustum of a Cone, the Bases being alike and alike situate, as in the precedent Examples, the Dimensions being,  
 A = 144 Inches, the diameter above,  
 B = 108 Inches, the diameter below,  
 P = 60 Inches, the Perpendicular,  
 Q. The Content in Ale Gallons?  
 P) A — B (= d.

.6 = q



$$88.6 = d$$

$$88.6 = d$$

$$88.6 = d$$

12 = the first Coefficient,

$$108 = B$$

648 = the second Coefficient,

$$108$$

$$108$$

$$864$$

$$1080$$

11664 = BB, third Coefficient.

These three divided severally by the Divisor proper to a Cone, as in the Table mentioned, viz. 359.05 they quote;

The first = .000334

The second = .180476

$$12.031680$$

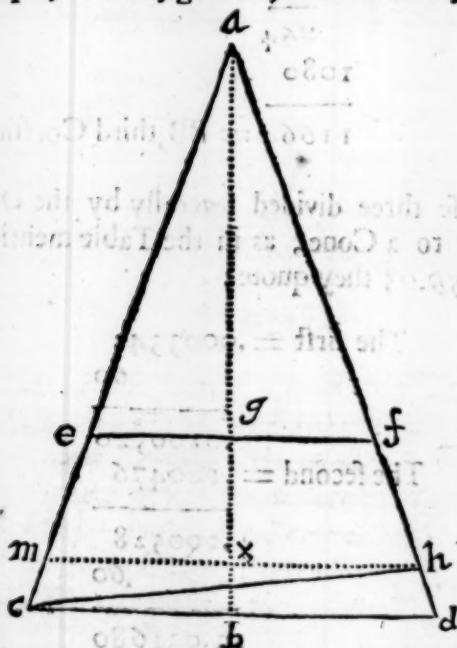
$$12.031$$

$$\begin{array}{r} 12.03168 \\ \text{The third} = 32.48572 \end{array}$$

$$\begin{array}{r} 44.51740 \\ -60 \\ \hline \end{array}$$

The Answer = 2671.0440 Ale Gall.

And that the young Gauger may not be obliged to Dray-men to repleat the horizon with liquor, of such Tunns whose Bases are not posited parallel thereto, (as indeed most are not being made with a Drip or Fall) let him take this Example,  $abcdefghmx$ , a Cone or Pyramid.



Having

Having the length of each Line in this Diagram, and the Content of the whole Cone or Pyramid in Cubick Inches, Gallons, or Barrels, &c. the Quantity of the Hoof  $hcb$  is found by this Analogy;

*As the Cube of the Line  $a c$ ,  
to the whole Solidity:*

*So is the Cube of a Geometrical Mean between  
 $a c$  and  $a h$ ,*

*to the Content of the Cone or Pyramid cut off:*

Which subducted from the whole, the remainder is the Content of the Hoof.

Some of the Lines being given, the rest are to be found.

*Example,*

*There is a Tunn taken as the Frustum of a Cone,*

*$c d = 144$  Inches, the greater Base,*

*$e f = 108$  Inches, the lesser Base,*

*$g b = 60$  Inches, the depth.*

Admitting the Base were raised 3 Inches, as the Line  $c h$ , it is then necessary to take another Diameter between  $c h$  and  $e f$  to find  $c d$ .

*To find  $a b$  the Cones Axe.*

*As 18, the semi-diff. of Diam. co. ar. 8,744728*

*to 72, the semi-diam. at the Base: 1,857332*

*So is 60, the Tuns depth, 1,778151*

*to 240, the Cones Axe.*

*2,380211*

*q. of  $a b$  240*

*5,760422 = 57600*

*q. of  $c b$  72*

*3,714664 5184*

*Log. of the Sum of their q. 4,797848*

*62784*

*The*

The Logarithm of  $ac$  250.567 2,398924

The Logarithm of  $ab$  247.567 2,393692

---

4,792616

A Geometrical Mean 2,396308

To find the Content of the whole Cone.

The Square of 144 4,316724

$\frac{2}{3}$  of  $ab = 80$  1,903090

359 &c. complement arithm. 7,444842

---

Content in Ale Gallons 4620 fere 3,664656

The Line  $ac$ , the Line  $ah$ , and the Content being known, to find the Content of the Fall  $cbdh$ .

As the Cube of  $ac$ , quare. ar. 2,803228

to the whole Content: 3,664656

So is the Cube of the Mean, 7,188924

to the Content of the Cone cut off. 3,656808

4537.4

4620

---

82.6 the Content of the Fall.

Or thus:

As the Cube of  $ac$ , ar. 2,803228

to the whole Cones Solidity: 3,664656

So is the Cube of  $ah$ , 7,181076

to the lesser Cones Solidity. 3,648960

---

4456 fere.

The whole Cone = 4620

---

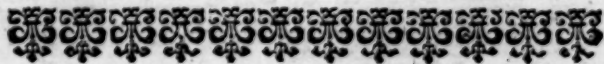
The Frustum  $mxhcb d = 164$

---

The being  $\frac{1}{2}$  the Fall or Hoof = 82



Some Practical  
RULES & EXAMPLES  
FOR  
*CASK-GAUGING.*



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FOR

CHAS. K. GARDNER

1009 5th Ave. New York, N.Y.



Some Practical

# RULES & EXAMPLES

FOR

## CASK-GAUGING.

**T**He Corner-stone in the whole Fabrick of Cask-Gauging, as full, was long since laid by Mr. *Oughtred*, taking a Cask to be the Frustum of a Spheroid, under which capacity they are generally received, though indeed there have been, and daily are found some Cask differing in form, and really are more Parabolical than Spheroidal, I shall therefore lay down a plain Method for the performance of the Work (*viz.* finding their Content) under these four Considerations:

As { Spheroidal,  
 { The Frustum of a Parabolical Spindle;  
 { The Frustum of a Parabolical Conoid,  
 { The Frustums of two Cones abutting  
 upon one common Base.

These



These severally, with and without a Table of Area's of Circles.

And forasmuch as the Dimensions must be the first thing known, before the Content can be found, I shall therefore shew the young Tyro, how by some of the Dimensions to find the rest, if any obstruction prohibit the taking of all.

*The Bounge-diameter, and Head-diameter, and Diagonal, to find the Casks length.*

First subduct the semi-difference of Diameters from the Bounge-diameter, and Square the Remainder, which Square subduct from the Square of the Diagonal, and the Remainder is the Square of the Casks semi-length.

*Example.*

Let BD be the Bounge-diameter = 29 Inches,  
 HE be the Head-diameter = 23 Inches,  
 BE be the Diagonal = 35.3836 Inches,  
 SD the semi-difference = 3 Inches :

Q. the Length = L T?

The Square of BE = 1252

Square of BD — SD = 676

Square of semi-length = 576

24

48 = LT.

This very Quest. was intended by Mr. Smith, p. 176. but through a Mistake it was left out.

*The*

The Bounding-diameter, Diagonal, and Length, to find the Head-diameter.

The Rule.

From the quadrupled Square of the Diagonal subduct the Square of the Length, (which done) the Square Root of the Remainder is equal to the Sum of the Bounding-diameter and one Head-diameter.

Example.

The Square of Diagonal = 5008

Square of the Length = 2304

Remainder = 2704  $\sqrt{\phantom{x}} = 52$

Subduct the Bounding-diameter = 29

Head-diameter = 23

The Head-diameter, Bounding diameter, and the Length, to find the Diagonal.

The Rule.

To the Square of the Semi-length add the Square of the Bounding diameter, less the Semi-difference of Diameters, and the Square Root of their Sum is equal to the Diagonal.

O

Example.

Example: *Find the Content of a Cask*

$$\text{Square of Semi-length} = 576$$

$$\text{Square of } 26 = 676$$

$$\text{Square of Diagonal} = 1252 \quad \sqrt{35.3836} >$$

A Cask taken as the Frustum of a Spheroid, cut with two Plane Parallels, each Plane bisecting the Axis at right Angles,

B the Boun-diameter = 29 Inches,

H E the Head-diameter = 23 Inches,

L T the Length = 48 Inches:

Q. The Content in Wine Gallons?

### The Rule.

To the doubled Square of the Boun-diameter, add the Square of the Head-diameter, their Aggregate multiply by the Length, and to the Product add the tenth part of it self, more one third of that tenth part, and from the Sum cut off as many places toward the right hand as were in the Multiplicand.

Example.

$$\text{The doubled Square of } 29 = 1682$$

$$\text{The Square of } 23 = 529$$

$$\text{The Aggregate} = 2211$$

# Practical Gauging.

135

$$\text{The Length} = 48$$

$$17688$$

$$8844$$

$$\text{The Product} = 106128$$

$$\text{Tenth} = 106128$$

$$\text{The } \frac{1}{30} \text{ part, or } \frac{1}{3} \text{ of } \frac{1}{10} = 35376$$

$$\text{The Answer} = 120.2784 \text{ Wine Gallons}$$

Another way.

$$\text{The q. of the Boun-diameter} = 841$$

$$\text{The q. of the Head-diameter} = 529$$

$$\text{The Sum of their Squares} = 1370$$

$$\text{The Semi-sum} = 685$$

$$\text{The Semi-diff. of Squares} = 156$$

$$\text{Their Aggregate} = 2211$$

$$\text{The Length} = 48$$

$$17688$$

$$8844$$

$$\text{The Product} = 106128$$

$$\text{The tenth part} = 106128$$

$$\text{The } \frac{1}{30} \text{ part or } \frac{1}{3} \text{ of } \frac{1}{10} = 35376$$

$$\text{The Answer in Wine Gall. } 120.2784$$

*The same Cask being taken as the Frustum of a Parabolical Spindle, the Content may be thus found.*

$$q. \text{ of the Boun-diameter} = 841$$

$$q. \text{ of the Head-diameter} = 529$$

$$\text{The Aggregate} = 1370$$

$$\text{The Semi-sum} = 685$$

$$\text{The tenth part of the Diff.} = 312$$

$$20862$$

$$\text{The Length} = 48$$

$$166896$$

$$83448$$

$$\text{The Product} = 1001376$$

$$\text{Tenth of the Product} = 1001376$$

$$\frac{1}{3} \text{ of } \frac{1}{10} = 333792$$

$$\text{The Answer in Wine Gall, } 113.48928$$

*If taken as the Frustum of a Parabolical Conoid, cut as before mentioned, the Content may be found as in this*

*Example.*

$$q. \text{ of the Boun-diameter} = 841$$

$$q. \text{ of the Head-diameter} = 529$$

$$\text{The Sum} = 1370$$

$$\begin{array}{r} 1370 \\ \text{Semi-sum} = 685 \\ \hline \end{array}$$

$$\begin{array}{r} 2055 \\ \text{The Length} = 48 \\ \hline \end{array}$$

$$\begin{array}{r} 16440 \\ 8220 \\ \hline \end{array}$$

$$\text{The Product} = 98640$$

$$\text{Tenth part of the Product} = 9864$$

$$\frac{1}{30} \text{ part, or } \frac{1}{3} \text{ of } \frac{1}{10} = 3288$$

$$\text{The Answer in Wine Gall. } 111.792$$

*If a Cask of the same Dimensions be taken as the middle Frustum of two Cones abutting upon one common Base, cut with two Planes parallel, and each bisecting the Axis at Right Angles, the Content in Wine Gallons may be found as in this*

*Example.*

$$q. \text{ of the Bounq-diameter} = 841$$

$$q. \text{ of the Head-diameter} = 529$$

$$\text{The Sum} = 1370$$

$$\text{The Semi-sum} = 685$$

$$2055$$

$$\text{Semi-q. of diff. of Diam.} = 18$$

$$2037$$



2037

48

16296

8148

97776

97776

32592

The Answer in Wine Gall. 110.8128

For finding the Capacity of these, or any other Vessels, it is convenient to have always in readiness a Table of Area's of Circles in Wine and Ale Gallons: I think it unnecessary to swell this intended small Volume with them, there being two lately Printed, exactly Calculated to every tenth part and quarter of an Inch, and also a Table of Area's of Segments of a Circle, by my good Friend Mr. *John Smith*, in his Book of *Gauging*, to whom in gratitude I am obliged to render my hearty acknowledgment for many favours and kind assistances in these Studies; yet that you may be able to find any Area of a Circle upon demand, in Wine or Ale Gallons, without a Table, take this

*Rule.*

Divide the q. of the Diameter by 294.1 for Wine, and by 359.05 for Ale Gallons, and the Quotient exhibits the Area. Or, saith Mr. *Smith*, Multiply the q. of the Diameter by .0034 for Wine



# Practical Gauging.

Wine, and by .003785 For Ale Gallons, and the Product exhibits the Area in such Gallons.

As in these Examples.

The Diameter of a Circle = 21.7: Q. The Circles Area in Wine Gallons?

$$\begin{array}{r}
 21.7 \\
 \times 21.7 \\
 \hline
 1519 \\
 217 \\
 \hline
 434 \\
 \hline
 294
 \end{array}
 \begin{array}{r}
 470.89 \\
 .0034 \\
 \hline
 188356 \\
 141267 \\
 \hline
 1.601026
 \end{array}$$

294 < 470.89 (1.601026) 1.601026  
 1768  
 ... 490

The Diameter of a Circle = 26.8: Q. The Area in Ale Gallons?

$$\begin{array}{r}
 26.8 \\
 \times 26.8 \\
 \hline
 2144 \\
 1608 \\
 \hline
 536 \\
 \hline
 359.05
 \end{array}
 \begin{array}{r}
 718.24 \\
 .00 \\
 \hline
 574 \\
 5027 \\
 14365 \\
 \hline
 2.0002
 \end{array}$$

For finding the Capacity of a Cask, taken as Spheroidal, by a Table of Areas of Circles in Gallons.

## Example.

A Cask's Bung-diameter = 29 Inches, Head-diameter = 23, and the Length = 48 Inches:

Q The Contents in Wine Gallons?

$\frac{2}{3}$  of the Area of the Bung  $\odot = .9531$

$\frac{1}{3}$  of the Area of the Head  $\odot = .5996$

Their Sum = 1.5527

Semi-sum = .7763

Semi  $\infty = .1768$

Area of Mean Circle = 2.5058

The Length = 48

200464

100232

The Answer in Wine Gall. 120.2784

## Another way.

$\frac{2}{3}$  of the Area of Bung  $\odot = 1.9062$

$\frac{1}{3}$  of the Area of Head  $\odot = .5996$

The Area of Mean  $\odot = 2.5058$

The Length = 48

200464

100232

The Answer = 120.2784

That is, 120 Gallons, 1 Quart, and  $\frac{1}{4}$  of a Pint,  
*scilicet*

To find the solid Content of a Cask, when taken  
as the middle Frustum of a Parabolical  
Spindle, &c.

The Dimensions as before.

$$\frac{1}{3} \text{ of the Area of Bung } \odot = .9531$$

$$\frac{1}{3} \text{ of the Area of the Head } \odot = .5996$$

$$\text{Their Sum} = 1.5527$$

$$\text{Semi-sum} = .7763$$

$$\text{Tenth of the Difference} = .03535$$

$$\text{Area of Mean } \odot = 2.36435$$

$$\text{The Length} = 48$$

$$1891480$$

$$945740$$

$$\text{The Answer in Wine Gall. } 113.48880$$

That is, 113 Gallons, and almost 2 Quarts.

And as the Frustum of a Parabolical Conoid,  
the Capacity is thus found:

$$\frac{1}{3} \text{ of the Area of the Bung } \odot = .9531$$

$$\frac{1}{3} \text{ of the Area of the Head } \odot = .5996$$

$$\text{Their Sum} = 1.5527$$

$$\text{Semi-sum} = .7763$$

$$\text{Area of the Mean } \odot = 2.3290$$

$$\text{The Length} = 48$$

$$18632$$

$$9316$$

$$\text{The Answer in Wine Gall. } 111.792$$

If a Cask be taken as the middle Frustum of two Cones, abutting upon one common Base, &c.

The Dimensions as before.

$$\frac{1}{3} \text{ of the Area of the Bounding } \odot = .9531$$

$$\frac{2}{3} \text{ of the Area of the Head } \odot = .5996$$

$$\text{Their Sum} = 1.5527$$

$$\text{The Semi-sum} = .7763$$

$$2.3290$$

$$\frac{1}{6} \text{ of Area of } \odot \text{ the } \odot \text{ of Diam.} = .0204$$

$$\text{The Area of Mean } \odot = 2.3086$$

$$\text{The Length} = 48$$

$$184688$$

$$92344$$

The Answer in Wine Gall. 110.8128

The Ullage, or Wants in a Cask, may be found under these two Considerations :

1. A Cask standing on the Head, with the Diameters parallel to the Horizon.

2. A Cask lying with the Axe parallel to the Horizon.

Prop. I.

In a Cask standing on the Head, with the Diameters parallel to the Horizon, some Liquor remaining, to find how many Wine Gallons it is.

Here

Here are these five things necessary to be known :

1. The Diameter at the Bounge.
2. The Diameter at the Head.
3. The Length of the Cask.
4. The Depth of the Liquor.
5. The Diameter of the Liquors superficies.

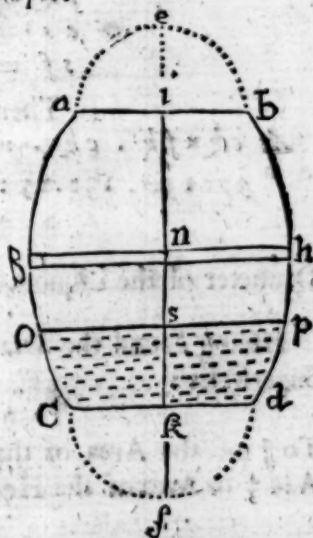
Example.

Let  $ghbe = 29$

$ab \& cd = 23$

$ik \dots = 48$

$sk \dots = 11.6$



The Diameter  $op$  is thus found, first find the Axis of the whole Spheroid  $ef$ , thus; from the Square of half the Bounge-diameter ( $nh$ ) subduct the Square of half the Diameter at the Head, and extract the Square Root of the Remainder: Then by the Rule of Proportion, say, As that  $q \sqrt{\phantom{x}}$ , is to  $nh$ , the Semi-bounge-diameter: So is  $ni$ , the Casks Semi-length, to  $en$  half the Axis sought.

$q.nh$

$$q. nb = 210.25$$

$$q. ai = 131.25$$

$$78.00 \sqrt{\phantom{x}} = 8.8311 >$$

$$As 8.8318 > .145 :: 24.39.4$$

$$Then is fe = 78.8$$

$$ek = 63.4$$

$$fk = 15.4$$

$$es = 51.8$$

$$sf = 57$$

Then,

$$As ek \times fk . ckq. :: es \times sf . sqq.$$

$$976136.132.25 :: 1398.6.13.7$$

$$15.7 sp$$

Diameter of the Liquors Superficies 27.4

Having found the Diameter of the Liquors Superficies :

Then,

$$To \frac{2}{3} \text{ of the Area of that Circle} = 1.70173$$

$$Add \frac{1}{3} \text{ of Area of the Head Circle} = .59953$$

$$2.30126$$

$$The Depth of Liquor = 11.6$$

$$1380756$$

$$230126$$

$$230126$$

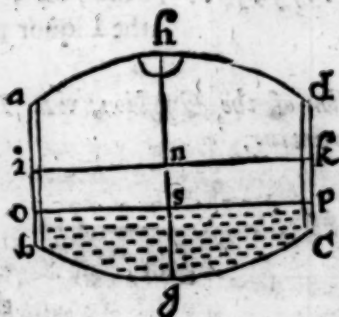
$$The Answer in Wine Gallons = 26.694616$$

Which subtracted from the whole Content,  
leaves the Ullage or Wants. Prop.



Prop. II.

A Cask lying with its Axe parallel to the Horizon, and having some Liquor remaining in it, to find the Contents of the said Liquor in Gallons.



Let the Dimensions be as before.

In this Proposition there is five Requisites attending :

$hg$  the Diameter at the Bounge = 29.

$ab$  the Diameter at the Head = 23.

$ik$  the Length = 48.

$sg$  the Depth of Liquor = 11.6.

And the Content of the whole Cask in Gallons.

Then by the help of a Table of Area's of Segments of a Circle, whose Area is Unity, and the Radius divided in the Ratio of 1.0000 Parts, say by the Rule of Proportion :

$hg$	$sg$	Radius	
As 29	. 11.6	:: 1.0000	. .4 versed Sine or Arrow of Segment. Then



Then seeking in the Table you will find .4000, and right against it under the Title *Area* you will find .37353. Then say:

whole Content  
 $1.0000 \cdot .37353 :: 120.2784 \cdot 44.9276$   
 the Liquor remaining.

*The Inversion of the Question, viz. To find the Liquor wanting.*

As 29 . 17.4 :: 1.0000 . .6

Again,

the Ullage.

As 1.0000 . .62647 :: 120.2784 . 75.3509  
 The Liquor remaining = 44.9276

Which together make 120.2785  
 the Casks whole Capacity.

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**FINIS.**

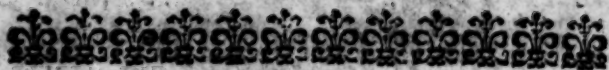
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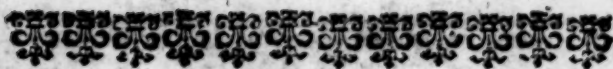
ERRATA.

**P** Ag. 3. l. 4. r. in the third. P. 5. l. 22. r.  
20:13. P. 7. l. 17. r. 42:3:08:15;  
l. 19. r. 33:0:05:04. P. 9. l. 1. r. borrow  
of the. P. 13. l. 14. r. 5 s. the bushel. P. 16.  
l. 13. r. 2 times. P. 19. l. 1. r. 5 from 6. P. 31.  
l. 19. ~~dele~~ always. P. 39. l. 22. r. in the deci-  
mal Fractions of both Factors. P. 50. l. 15. r.  
solid measure. P. 51. l. 15. r. 272.25. P. 52.  
l. 15. r. .0041667. P. 67. l. 14. ~~dele~~ as before.  
P. 82. l. 14. r.  $\div a$ . P. 188. l. ult. r.  $\frac{1}{2}$  being.

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**T**He Rules herein mentioned, and  
other Mathematical Arts, are taught  
by the Author, viz. Arithmetick, Vul-  
gar, Decimal, and Logarithmetical;  
the Doctrine of Triangles, Plain and  
Spherical; the Use of the Globes, Qua-  
drant, Sector, and other Mathematical  
Instruments; Fair Writing, and Mer-  
chants Accompts, by way of Debitor and  
Creditor; also the Art of Short Wri-  
ting.



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